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Extension of the SCEC Broadband Platform to Simulation of Strong Ground Motions from Subduction Earthquakes

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Objective

The objective of this project is to develop the software infrastructure for extending the applicability of the SCEC Broadband Strong Ground Motion Simulation Platform (BBP) to subduction earthquakes. This will be done by performing a test application of the software to a subduction earthquake.

This project was motivated by a request from Professor Brendon Bradley, co-leader of the New Zealand QuakeCoRE: Centre for Earthquake Resilience, for the PI's to participate in a project entitled "Validation of Strong Ground Motion Simulations of two Historical New Zealand Subduction Zone Earthquakes on the SCEC Broadband Strong Ground Motion Simulation Platform." To date, the SCEC BBP has only been developed for use in simulating the strong ground motions of shallow crustal earthquakes. Professor Bradley has expressed the desire that the validations be performed within the framework of the SCEC BBP, and suggested that we seek funds from SCEC to perform preparatory work for extending the SCEC BBP capability to subduction earthquakes in readiness for the New Zealand project. That project, which included collaboration with Professor Bradley, has been completed and the report is attached at the end of this report. This project represents a strategic partnership between QuakeCoRE and SCEC that will develop long-lasting mutual benefits for both organizations.

Method

We chose the 2011 Mw 9.0 Tohoku earthquake for this purpose because we have already performed 1D and 3D ground motion simulations (Skarlatoudis et al. 2015a) of that earthquake outside the SCEC BBP, providing a means to verify the results of our simulations. The project involved the following activities:

We used a 1D seismic velocity structure model (Table 2) for the Tohoku region derived from the Koketsu et al. (2008) Japan Integrated Velocity Structure Model (JIVSM). We generated 1D Green's functions for the long period component of the simulations using this seismic velocity model.

We adapted the Graves & Pitarka (2015) rupture generator to subduction earthquakes using recently developed earthquake source scaling relations for subduction earthquakes (Skarlatoudis et al., 2015b). We have shown, for example, that the relation between seismic moment and fault rupture area, and the corner periods of the along-strike and downdip wavenumber spectra, are different between these two categories of earthquakes. We used these scaling relations to modify the G&P2014 rupture generator, which is for crustal earthquakes, for use with subduction earthquakes.

We developed an earthquake rupture file based on the fault model of the 2011 Tohoku earthquake and used it to run the simulations. We calculated the response spectra of the recorded ground motions and corrected them for site response using the site amplification factors for Japan developed by Boore et al. (2014). We then measured the response spectral goodness of fit of the simulations to the data.

The Kurahashi and Irikura (2011) earthquake source model that we used for the Mw 9.0 Tohoku earthquake ground motion simulations is shown in Figure 1. The source parameters of the model are

listed in Table 2. We used this model to test our implementation of subduction strong motion simulation on the BBP.

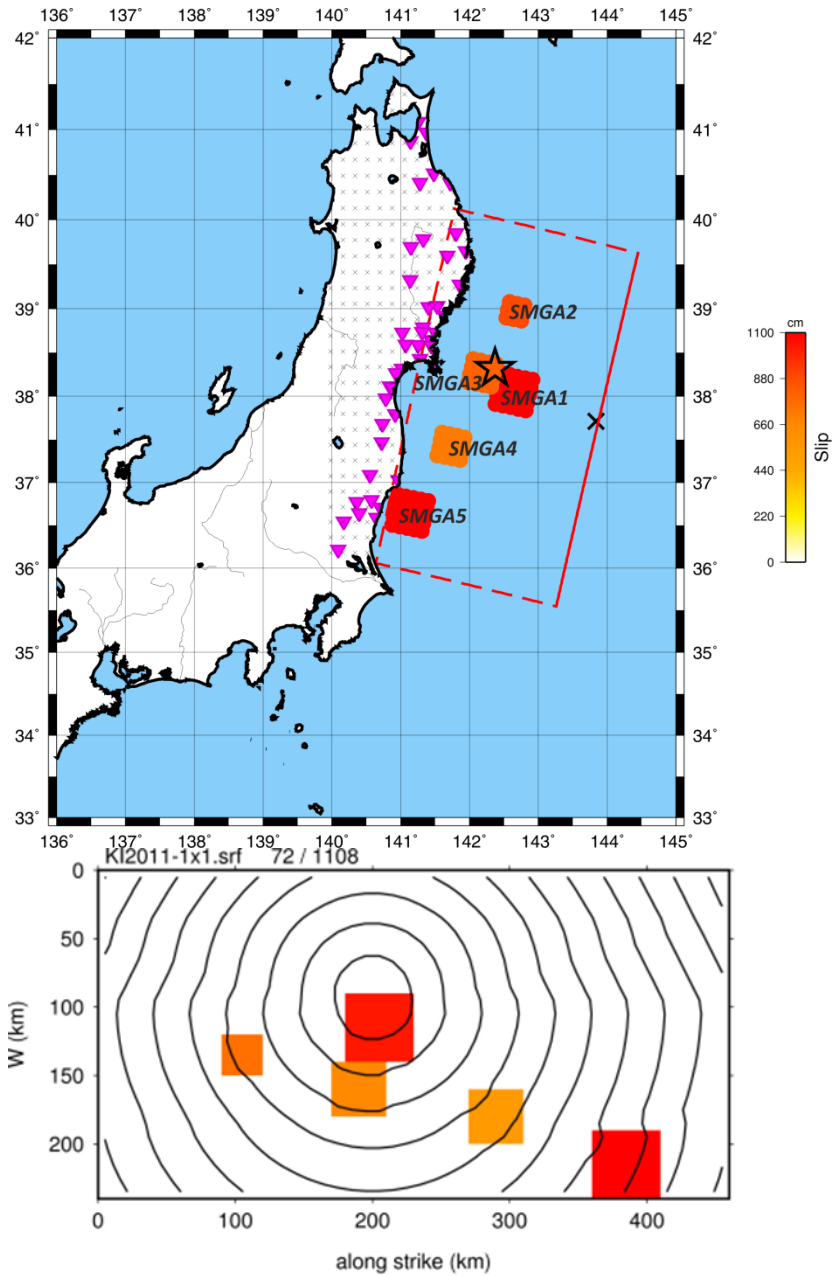


Figure 1. Top: Rupture model of the **M** 9.0 Tohoku, Japan earthquake 2011, showing the slip distribution of Kurahashi and Irikura (2011), the locations of strong ground motion recording stations, and the grid of stations used for simulations. Bottom: Resampled rupture model used in the calculations. Slip values (in cm) indicated by red shading. Contours of rupture initiation times across the fault plane are shown at 5s intervals. Source: Skarlatoudis et al., 2015c.

Table 1. Seismic Velocity Model for Tohoku.

Thickness (Km)	Vp (m/s)	Vs(m/s)	Density (kg/m ³)	Qp	Qs
0.002	1700	450	2	45	22.5
0.004	1800	650	2.1	65	32.5
0.006	1800	850	2.1	85	42.5
0.008	1900	950	2.1	95	47.5
0.01	2000	1150	2.2	115	57.1
0.07	2400	1200	2.2	120	60
0.1	2600	1300	2.4	130	65
0.16	3000	1400	2.45	140	70
0.1	3600	2000	2.55	200	100
0.44	4200	2400	2.6	240	120
5.9	5500	3200	2.65	320	160
10.2	6100	3400	2.75	340	170
14.63	6500	3800	3	380	190
16	7800	4500	3.3	450	225

Table 2. Source Parameters of the Kurahashi and Irikura (2011) Model of the Tohoku Earthquake

	L (km)	W (km)	M ₀ (Nm)	Stress Drop (MPa)	Delay from origin time (s)
<i>SMGA 1</i>	<i>62.40</i>	<i>41.60</i>	<i>2.31E+21</i>	<i>41.3</i>	<i>15.64</i>
<i>SMGA 2</i>	<i>41.60</i>	<i>41.60</i>	<i>7.05E+20</i>	<i>23.6</i>	<i>66.42</i>
<i>SMGA 3</i>	<i>93.60</i>	<i>52.00</i>	<i>4.34E+21</i>	<i>29.5</i>	<i>68.41</i>
<i>SMGA 4</i>	<i>38.50</i>	<i>38.50</i>	<i>3.83E+20</i>	<i>16.4</i>	<i>109.71</i>
<i>SMGA 5</i>	<i>33.60</i>	<i>33.60</i>	<i>3.99E+20</i>	<i>26.0</i>	<i>118.17</i>

The goodness of fit of our broadband strong motion simulations to the response spectra of the Mw 9.0 Tohoku earthquakes obtained on our own computers in previous work (Skarlatoudis et al., 2015) is shown in Figure 2. There is little systematic bias in the prediction of the ground motions in the period range of 0.1 to 10 seconds, although there is some underprediction at a period of 0.5 seconds.

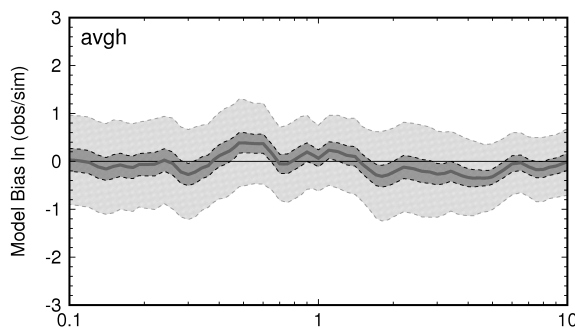


Figure 2. Goodness-of-fit (GOF) of recorded and simulated response spectra for the period range 0.1-10s for the 2011 Tohoku earthquake. The solid line shows the bias in natural log units; the light grey zone shows the standard deviation, and the dark grey zone shows the 90% confidence interval of the mean. Source: Skarlatoudis et al., 2015c.

The standard deviations of the predictions, shown by the grey shading, are about a factor of 1.5 (0.4 natural log units). This standard deviation is significantly less than the factor of 2.0 (0.7 natural log units) in current ground motion prediction equations (GMPE's) for subduction earthquakes (Abrahamson et al., 2015), as shown in Figure 3, demonstrating the advantage that strong motion simulations of subduction earthquakes can have over GMPE's in estimating ground motions for engineering applications.

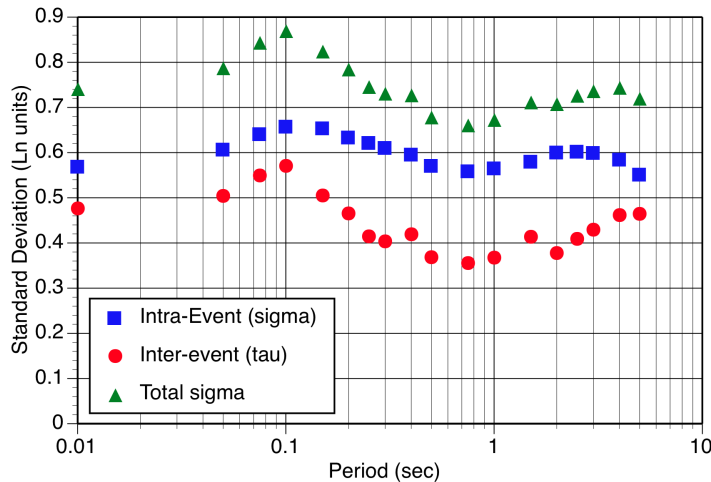


Figure 3. Standard deviation of the intra-event, inter-event and total variability as a function of response spectral period. Source: Abrahamson et al., 2015.

The simulation results generated on our computers and shown in Figure 2 were generated using a preferred rupture model for the event. However, the protocol used in the SCEC BBP validation procedure is to use a large set of randomly generated rupture models, initially 50 but since modified to 32 or 16, in order to include the uncertainty in the rupture models of future earthquakes. This obviates the need to account for uncertainty in the rupture model of future earthquakes when the BBP is used to estimate the ground motions of future earthquakes.

Figure 4 shows the goodness of fit in the period range of 1 to 10 seconds that was obtained by doing the simulations on the SCEC Broadband Platform. There is no significant bias in this period range.

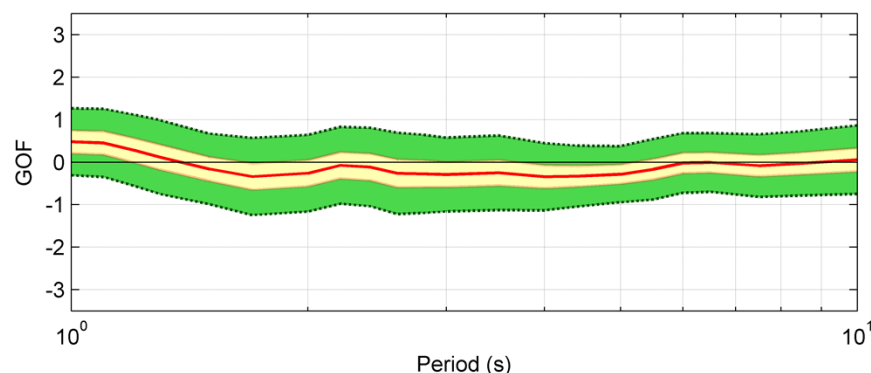


Figure 4. Goodness-of-fit (GOF) of recorded and simulated response spectra for the period range 0.1-10s for the 2011 Tohoku earthquake simulations on the SCEC Broadband Platform. The red line shows the bias, the light green zone shows the standard deviation, and the dark grey zone shows the 90% confidence interval of the mean.

The short-period (0.1 to 1 sec) component of the simulations done on our computers (Figure 2) used a method (Somerville, 1993) that is not available on the SCEC Broadband Platform. Consequently, we did not generate short-period ground motions on the SCEC Broadband Platform (Figure 4). The validation studies that we did for two New Zealand subduction zone earthquakes for the QuakeCoRE Project (see Appendix) indicate that the short-period component of the Graves & Pitarka (2015) simulation method will need to be modified to provide for broadband simulations for subduction earthquakes.

Guidance on Subduction Earthquake Ground Motion Simulations on the SCEC Broadband Platform

The simulations were performed using the Graves and Pitarka (2010) method as implemented in the SCEC BBP. The execution of the code was performed at the University of Southern California high performance computing system.

The implementation of the Graves and Pitarka (2010) method in the SCEC BBP enables the user to generate a finite-fault kinematic rupture model. The procedure then computes low frequency and high frequency synthetic time series, which are combined using a matched filter technique. SCEC BBP Platform (version 16.5.0) is by default set for the simulation of crustal events. To test the SCEC BBP's capability and adaptability to simulate subduction events, we simulated the ground motions of the 2011 Tohoku M9.0 earthquake using the original settings for Central Japan. In our simulations, we did not generate a suite of source models but instead used the source model obtained from inversion of ground motion parameters for Tohoku the earthquake (Wei et al. 2011). Otherwise, the procedure for completing the simulations was the same as the standard method used for Japanese crustal events on the BBP. The source model contains slip history information for each sub fault including total slip, rise time, and rake which together form the source time function of that sub fault. This version of the code uses 1D Green's functions and theoretical radiation patterns to propagate the fault plane source functions and generate the low-frequency portion of the ground motion at a specific station. We used the 1D Green's functions generated by Somerville et al. (2013) for the Japan region. For the simulation of the low frequency portion of the ground motions, theoretical Green's functions (GFs) are pre-calculated for the required source-to-site distances and depths. Green's functions are generated using a representative 1D velocity model for the Japan region, which is provided in Somerville et al. (2013).

The high frequency simulation approach is based on a method formalized by Boore (1983). Its application to finite-fault simulations is described by many authors such as Frankel (1995), Beresnev and Atkinson (1997), and Hartzell et al. (1999). The BBP high frequency simulation using Graves and Pitarka (2010) techniques requires parameters related to corner wavenumbers which currently are hardwired in the BBP. More details regarding adjusting the BBP settings to simulate ground motions can be found in Hosseini et al. (2016). Based on the validation studies that we did for two New Zealand subduction zone earthquakes for the QuakeCoRE Project (see Appendix), we do not recommend the use of the high frequency portion for subduction earthquake simulations using the SCEC BBP version 16.5.0, without adjusting the associated parameters.

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Appendix. AECOM QuakeCoRE Report, 2017.

PROJECT REPORT

**VALIDATION OF STRONG GROUND MOTION SIMULATIONS OF TWO
HISTORICAL NEW ZEALAND SUBDUCTION ZONE EARTHQUAKES ON THE SCEC
BROADBAND STRONG GROUND MOTION SIMULATION PLATFORM**

Prepared for:

QuakeCoRE

January 27, 2017



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Validation of Strong Ground Motion Simulations of two Historical New Zealand Subduction Zone Earthquakes on the SCEC Broadband Strong Ground Motion Simulation Platform

Introduction

In this project, we perform simulations of the ground motions from two historical New Zealand earthquakes using the Southern California Earthquake Center (SCEC) Broadband Strong Ground Motion Simulation Platform (BBP).

Our first case study is the 1931 Hawke's Bay earthquake. Hull (1990) concluded that this earthquake was a blind thrust fault in the accretionary prism of the subduction zone, not on the plate boundary itself. This earthquake was not recorded on strong motion instruments, but there is a detailed intensity map and we measure goodness of fit to the intensities by converting the results of our simulations to intensities. This earthquake is included because we consider that our modeled strong ground motion simulations may provide a useful basis for modeling the ground motions from large subduction earthquakes on the Hikurangi Trench. Secondly, we study the 15 July 2009 Mw 7.57 Fiordland earthquake. This earthquake occurred on the Puyesgur subduction zone at the southwestern end of the South Island (Beavan et al., 2010; Fry et al., 2010; Mahesh et al., 2011). The Mw 7.57 earthquake and a smaller earthquake (Mw 7.2) that occurred in 2003 were widely recorded on strong motion instruments.

In a related project, funded by SCEC, we have extended the BBP Graves and Pitarka (2015; GP2015 hereafter) hybrid simulation method to subduction events. Before this project, the BBP Graves & Pitarka method of combining low frequency synthetic seismograms and high frequency partly stochastic simulations had only been applied to shallow crustal earthquakes. In the past, at AECOM (formerly URS,) we have used a different hybrid method in which the long period simulations are done following GP2015, but the short period simulations were done using empirical source functions (Somerville et al., 1991; Somerville, 1993). In the BBP subduction implementation, we replace that method with the stochastic method used by GP2015. Using the SCEC BBP version of GP2015, we reproduced our previous validation of the procedure for the 2011 Tohoku earthquake. The validation shows little systematic bias in the prediction of the ground motions in the period range of 1 to 10 seconds. Further work is required to reduce the bias observed in the high frequency part (0.01 to 1s).

Hawke's Bay Earthquake Simulations

The historical 1931 Hawke's Bay earthquake, also known as the Napier earthquake, caused extensive damage and loss of life. Hull (1990) concluded that this earthquake was a blind thrust fault in the accretionary prism of the subduction zone, not on the plate boundary

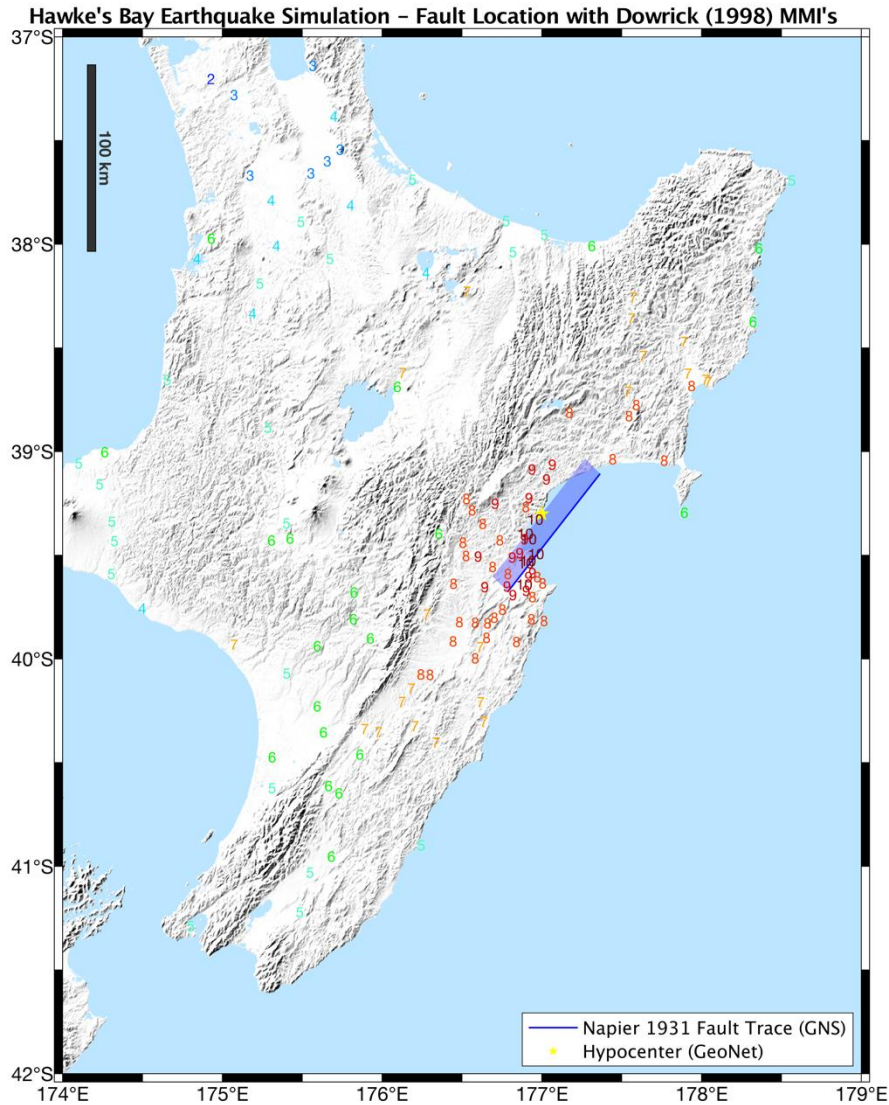


Figure 2. Region map of the north island, with the surface projection of the simulated fault plane in blue, hypocenter location marked by a gold star, and the Dowrick (1998) MMI values denoted on the map.

Simulation Results

We use the SCEC BBP version of GP2015 to create a source model using the parameters defined above (Figure 3), and perform simulations at each MMI location within Rjb distance of 100 km. We obtain three-component simulated acceleration time series at each site of interest. The strong motion simulations are adjusted for site effects using a Vs30-based empirical model applied to the Fourier amplitude spectra. Approximations for Vs30 at each site are obtained from topographic slope maps provided by the USGS (<http://earthquake.usgs.gov/hazards/apps/vs30/>).

The simulations are converted to intensity using the ground motion intensity conversion equation (GMICE) of Caprio et al. (2015), which is based on the PGA, PGV and geographic

region. The spatial distribution of the MMI residuals (Figure 4) does not exhibit in general any significant trends. The converted intensity values from the simulations are in a good agreement with the MMI observations throughout the distance range examined and no strong trends with Vs30 are observed (Figure 5 through Figure 8).

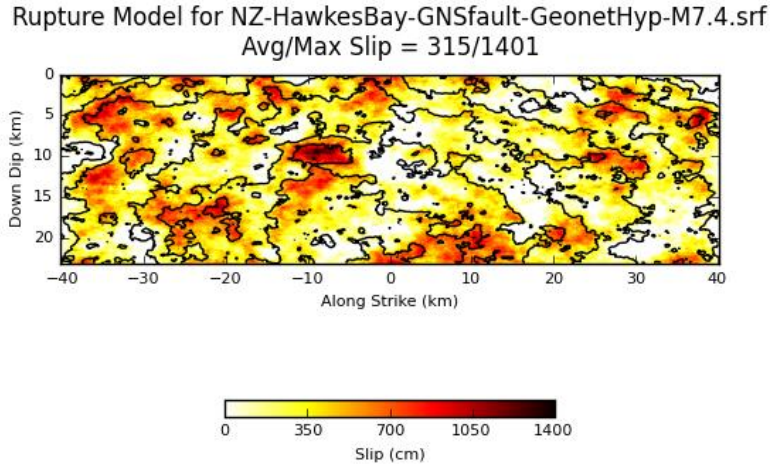


Figure 3. Illustration of the rupture model used for the Hawke’s Bay simulation.

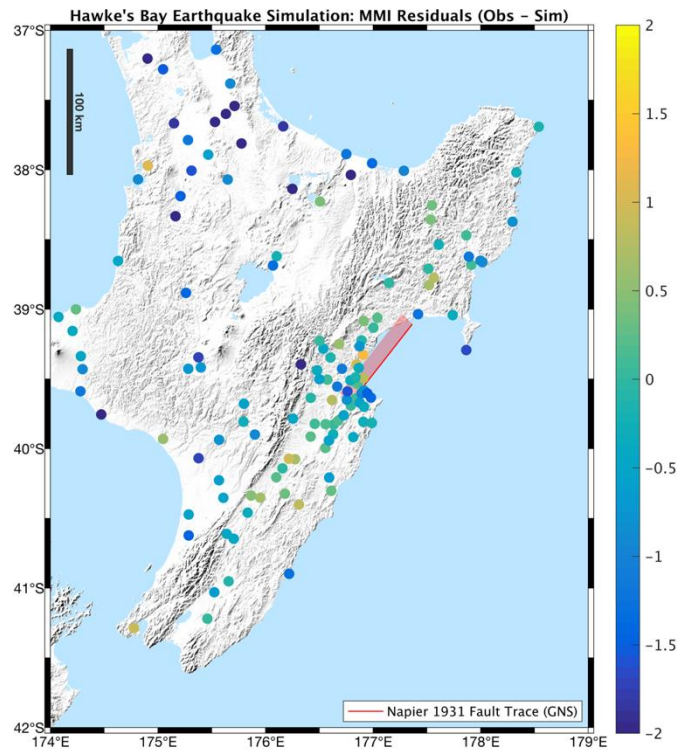


Figure 4. Spatial distribution of simulation MMI residuals.

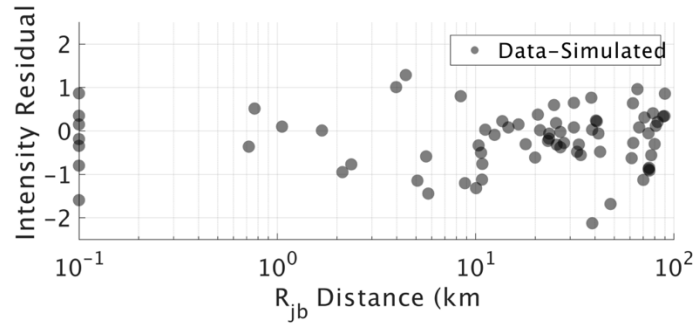


Figure 5. MMI intensity residuals versus distance.

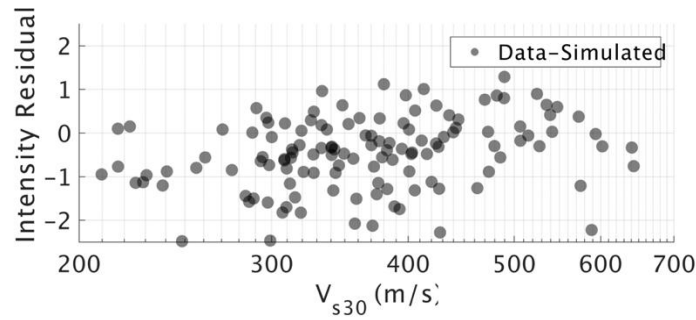


Figure 6. MMI intensity residuals versus Vs30.

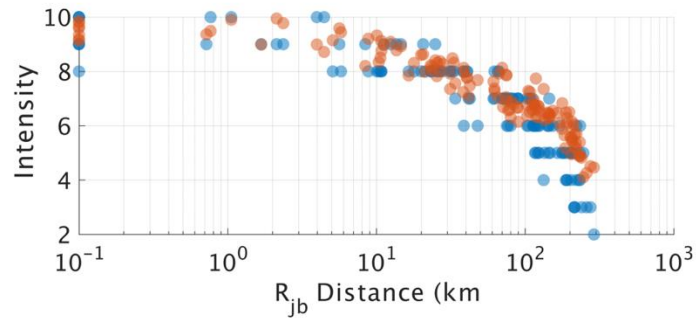


Figure 7. MMI versus distance. Dowrick (1998) values are in blue, and simulated values are in red.

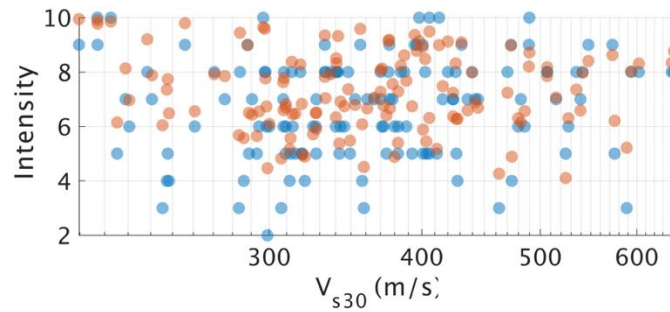


Figure 8. MMI versus Vs30. Dowrick (1998) values are in blue, and simulated values are in red.

Fiordland Earthquake Simulations

The 2009 Fiordland earthquake, also known as the Dusky Sound earthquake, occurred on the Puyesgur subduction zone at the southwestern end of the South Island (Beavan et al., 2010; Fry et al., 2010; Mahesh et al., 2011). This earthquake and a smaller earthquake (Mw 7.2) that occurred in 2003 were widely recorded on strong motion instruments. We use the SCEC BBP version of GP2015 to perform simulations of this subduction earthquake.

Seismic Velocity Model

We develop a generic 1D seismic velocity and density model for the Dusky Sound region of the south island (Figure 9). This model is created by averaging profiles from the Eberhart-Phillips et al. (2010) model sampled from the region with MMI VII in Fry et al., (2010). The s-wave velocities are modified in the upper 1.5 km to have a smooth transition to $V_{s30}=863$ m/s. For the long period component of the simulations, we calculate 1D Green's functions using this velocity model, and upload them to the SCEC BBP.

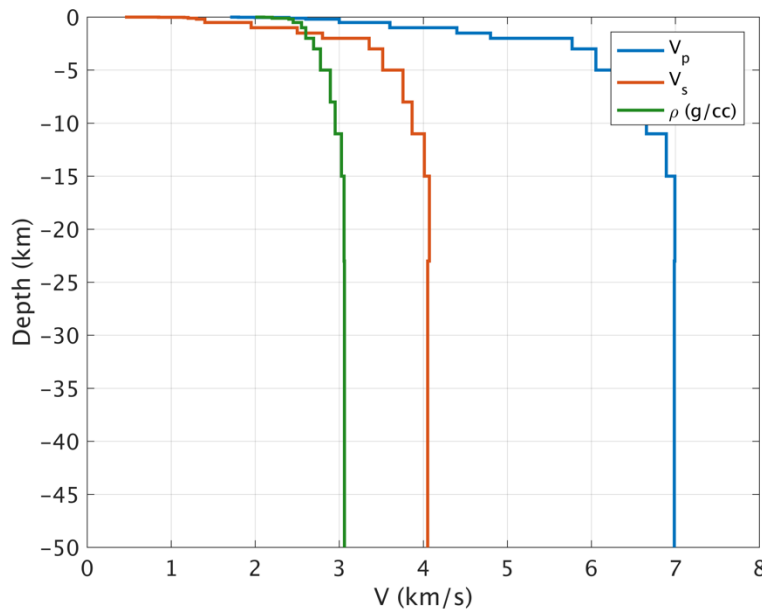


Figure 9. The 1D seismic velocity model used to represent the Dusky Sound region

Earthquake Source

Per GeoNet (geonet.org.nz), the earthquake rupture started at about 30 km depth and ruptured upwards and to the south, focusing energy offshore. Others (e.g. Fry et al., 2010; Gavin Hayes of USGS, personal communication) also report rupture propagating to the south with a strong slip asperity southwest of the hypocenter. We have selected the slip model from Gavin Hayes (USGS, personal communication) which has Mw 7.82, fault length 120 km, fault width 55 km, depth to the top of rupture 4.32 km, strike of 29 degrees, and dip of 26 degrees. Figure 10 shows the final slip distribution on the fault plane, and Figure 11 shows a map view of the surface projection of the fault.

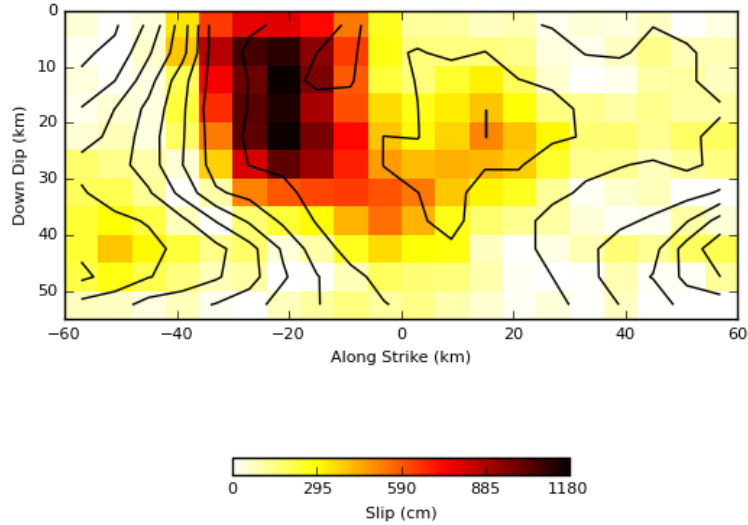


Figure 10. Illustration of the rupture model for the Fiordland simulation. The hypocenter is at approximately 20 km depth, to the northeast of the main slip asperity.

Simulation Stations

We select the nine stations south of latitude -44° and west of longitude 169° , where the strongest motions were recorded. These stations are identified in Figure 11, with the color scale denoting the recorded PGA.

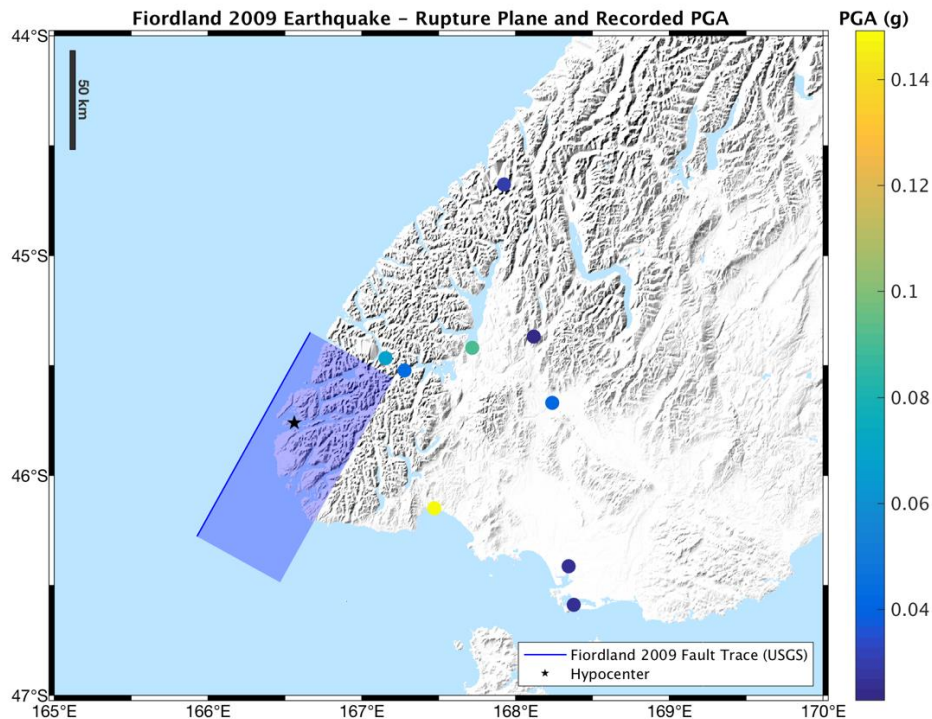


Figure 11. Map of the simulation region, with the surface projection of the simulated fault plane in blue, hypocenter location marked by the black star, and recording stations identified by colored circles. The color of each station is scaled to the recorded PGA.

Simulation Results

We use the SCEC BBP version of GP2015 to create a source model using the parameters defined above, and perform simulations at nine simulation stations. We obtain three-component simulated acceleration time series at each site. The strong motion simulations are adjusted for site effects using a Vs30-based empirical model applied to the Fourier amplitude spectra. Approximations for Vs30 at each site are obtained from topographic slope maps provided by the USGS (<http://earthquake.usgs.gov/hazards/apps/vs30/>).

We calculate response spectra (5% damped, RotD50 component) of the simulated acceleration time series and the recorded time series. The results are summarized in a goodness-of-fit (GOF) plot, shown in Figure 12. In Figure 12, the red line is the mean natural log residual over the nine simulated stations, and the green bands represent plus and minus one standard deviation from the mean. The yellow band represents the 90% confidence interval on the mean. This figure shows that, outside the range of 1-3 seconds, our simulations are over-predicting the ground motions. For high frequencies (periods shorter than 1 second), the simulation method is based on the stochastic method, and there are parameters which need to be tuned. These parameters include the high-frequency stress parameter (set to 50 bars), the damping model, and diminution parameter kappa, among others. We would like to explore the effect of these parameters in future research, to tune them, and preferably create regionalized rules for GP2015.

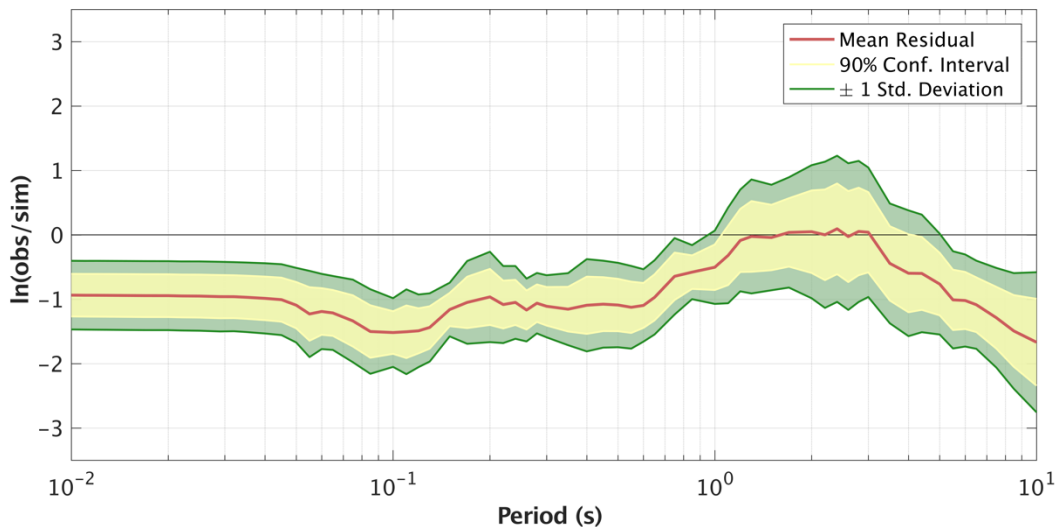


Figure 12. RotD50 component response spectra goodness-of-fit.

Figure 13 through Figure 16 show a comparison of the simulated and recorded RotD50 versus Rjb distance at four spectral periods. In Figure 17 the T=3.0s residuals are shown spatially; however, no trend with azimuth is observed.

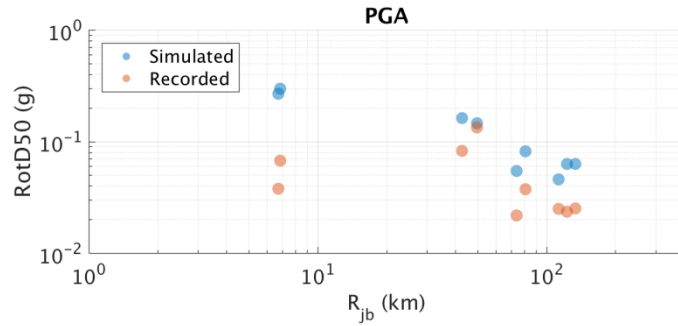


Figure 13. Simulated (blue) and observed (red) PGA versus distance.

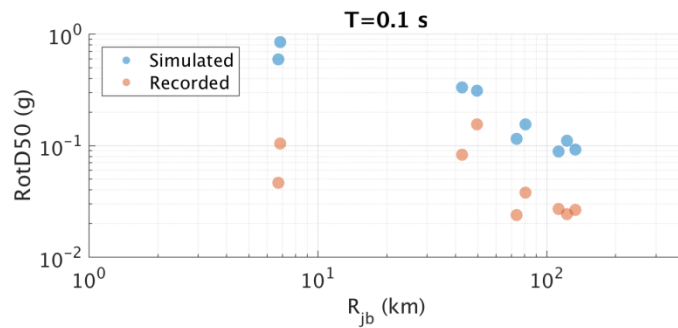


Figure 14. Simulated (blue) and observed (red) RotD50 at T=0.1s versus distance.

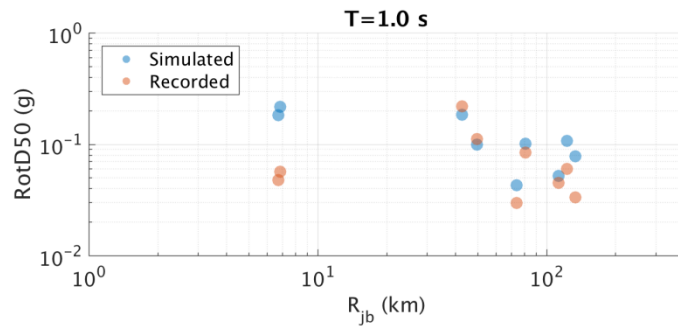


Figure 15. Simulated (blue) and observed (red) RotD50 at T=1.0s versus distance.

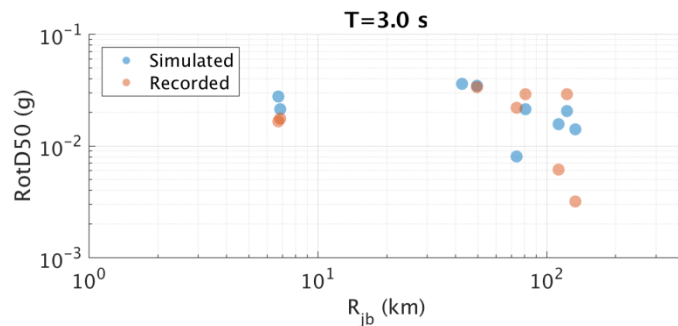


Figure 16. Simulated (blue) and observed (red) RotD50 at T=3.0s versus distance.

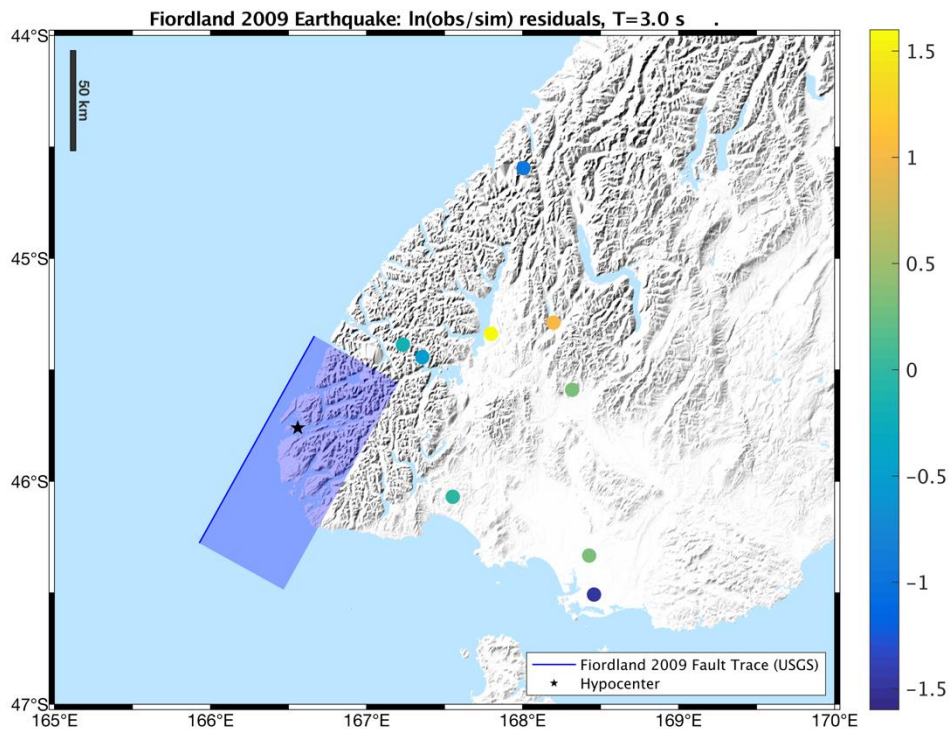


Figure 17. Map of the simulation region with color coded residuals for RotD50 at T=3.0s.

Conclusions

Using MMI as the intensity measure, the Hawke’s Bay simulations produced comparable predictions to the records compiled by Dowrick (1998). We did not observe any strong bias or trends in the MMI residuals with distance or Vs30. Although this earthquake was not modeled as a subduction earthquake, we anticipate that our simulations may provide a useful basis for modeling the ground motions from large subduction earthquakes on the Hikurangi Trench in the future.

For the Fiordland simulation, we calculated response spectra from the simulated waveforms. We observe the same behavior from our previous validation of the 2011 Tohoku earthquake: that further work is required to reduce the RotD50 bias observed in the high frequency part (0.01 to 1s) of GP2015 for subduction earthquakes. In this case, we are simulating significantly larger ground motions than those which were recorded. In the future, we would like to study additional events, and perhaps more generalized source models for this same event, to tune the high frequency parameters and create regionalized rules for them. Simulating more events will also allow us to better evaluate the performance of the simulation method at low frequencies by having a larger sample size from which to draw conclusions.

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