

### *Details of the Test*

**Consistency Tests**

- Check if the process is consistent with the hypothesis
- Based on Log-likelihood
- Concise & Intuitive Results
- Statistical Power
- Test for Normality
- Test for Outliers

**Comparison Tests**

- Compare two or more datasets
- Student's t-test
- Wilcoxon signed rank test
- Mann-Whitney U test

**Power of the Test**

Goal: How to compare test work with the data!

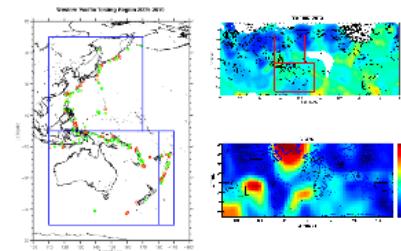
Test size =  $\alpha$  (Type I error rate)

Power =  $1 - \beta$  (Type II error rate)

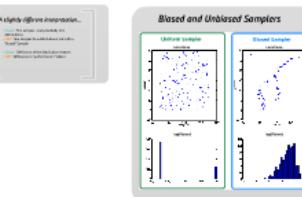
Type I error rate = probability of rejecting the null hypothesis

Type II error rate = probability of failing to reject the null hypothesis

## *Bonus Tracks*



Bonus Tracks



*Unfinished Business*

CSEP West Pacific

- 2 years of data are not enough, addition 1 year periods will be added
  - 3 models are a start but not enough
  - Magnitudes bins are missing and successor test regions like the global test region should consider them.

*Accounting for Uncertainties*

- The effect on the test outcome is dependent on the forecast and the location of the earthquakes
  - Can help to evaluate the robustness of forecast for a certain test region and time period
  - Uncertainty estimation is a valuable addition to the test procedure

*West Pacific Testing Region*

Setup

- Two sub-regions for testing NW and SW Pacific
  - Current 2 one-year periods are used (2009 and 2010)
  - Poisson rate forecasts from 3 Models:
    - DBM: Double-Branching Model by Marqueschi and Lombardi
    - KISS: Kagin and Jordan Smoothed Seismicity Model
    - Triple: Simple Smoothed Seismicity Model by Zechar and Jordan
  - Location uncertainties CMT: 10km

### *Test Results*



Uncertainties in RELM

stud

- Rework of the REHM experiment with uncertainty estimates
  - 5 forecast models:
    - Bill & Liu
    - Ebel et al.
    - Heinricher et al.
    - Koglin et al.
    - Shen et al.
  - Used catalog uncertainty
    - Location uncertainties: 5 km
    - Magnitude uncertainty: Laplace with sigma = 0.1 and 0.3
  - The ANSS-Catalog did change between evaluation and this review

## Results



## *Testing of Forecasts*

## Consistency Tests

- ```

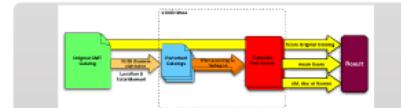
graph TD
    A[Check both factors are consistent with the algorithm?] -- Yes --> B[Calculate average]
    A -- No --> C[Get rid of one factor]
    B --> D[Add both factors]
    B --> E[Divide by total]
    D --> E

```

Power of the Test

- 

## *Uncertainty estimation*



- Symmetric uncertainties in MO - asymmetric uncertainties in Mw
- Because of Gutenberg-Richter Law there are more earthquakes below the magnitude threshold
- **BUT**, no higher probability for more earthquakes in the test regions was observed.

## *Motivation:*

- Estimation of the uncertainties of the tests
  - Measure the stability of the forecast models

## Accounting for catalog uncertainties: Western Pacific and RELM

# Accounting for catalog uncertainties: Western Pacific and RELM

David Eberhard

*SED ETH Zurich*

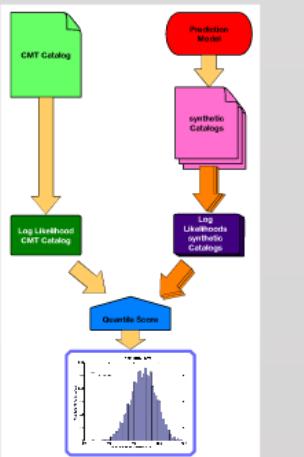
# ***Motivation:***

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# Testing of Forecasts

## Consistency Tests

- Check if the forecast is consistent with the observation
- Come in different "flavors"
  - L(ikelihood)-test
  - S(patial)-test
  - M(agnitude)-test
  - N(umber)-test



## Comparison Tests

- Compare forecasts and decide which performs better
- Based on rate-corrected average information gain per earthquake
- Two versions used:
  - Student's T-test (T-test)
  - Wilcoxon signed rank test (W-test)

## Power of the Tests

### "Test of the Tests":

Question: Do the comparison tests work with these data?

#### Error Type I

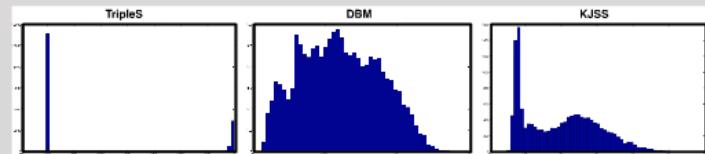
- Pick two random samples from the same forecast.
- Use the W-test and the T-test to determine if the samples are from the same forecast
- Do this several times to do some statistics

#### Error Type II

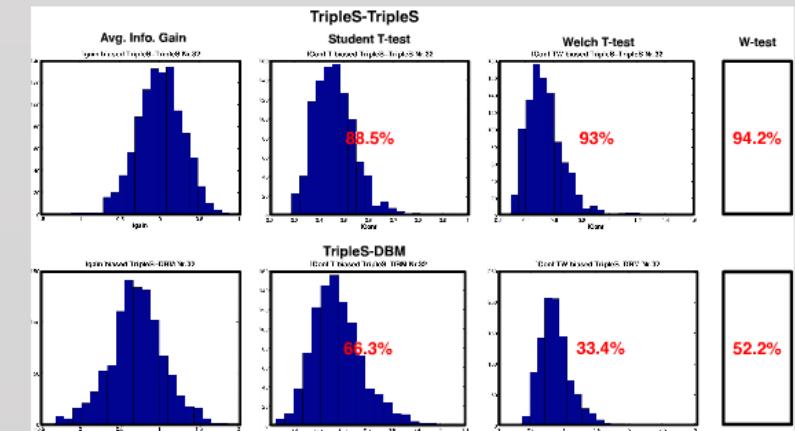
- Similar but use two "different" forecasts

Two "samplers" were used, a random and a "biased" one

#### Typical forecast distributions

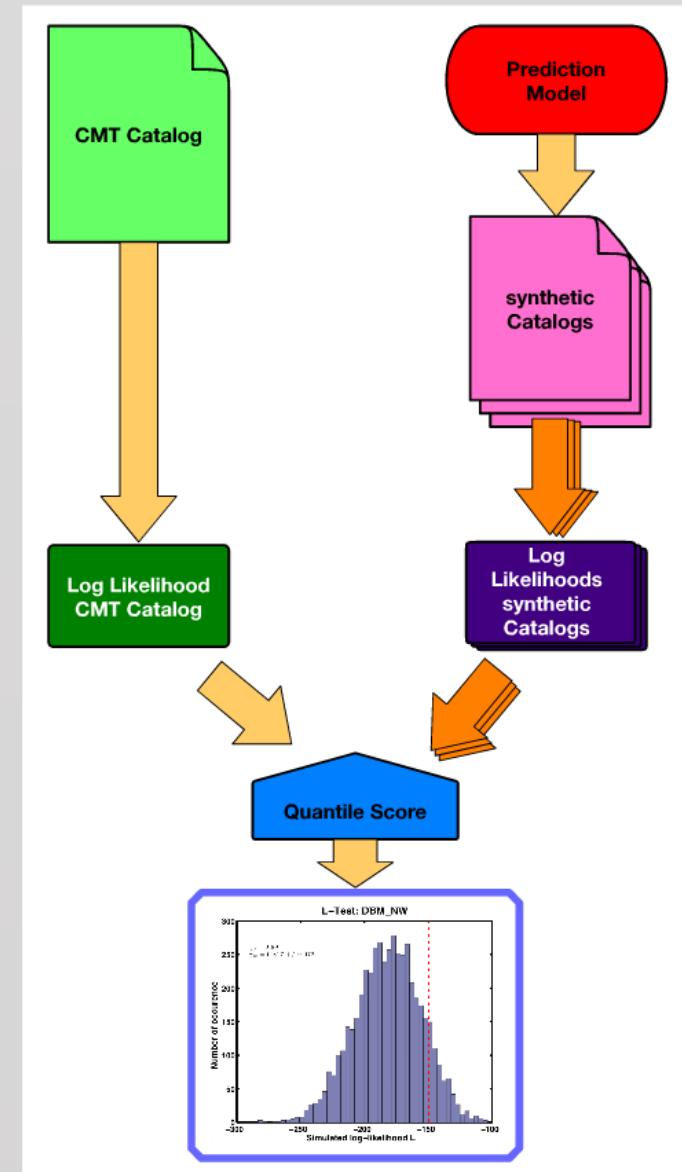


Example of log(A) distribution (NW Pacific 2009)



# *Consistency Tests*

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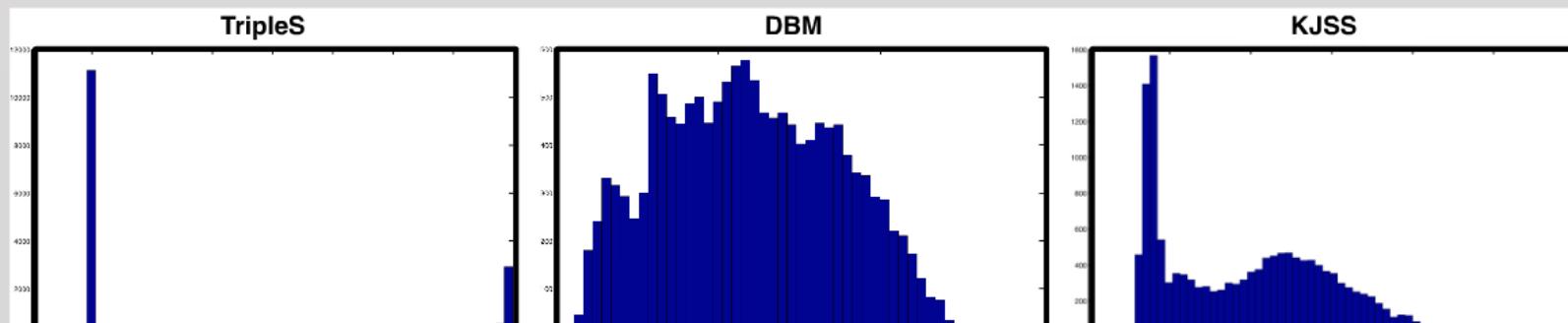
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*Typical forecast distributions*

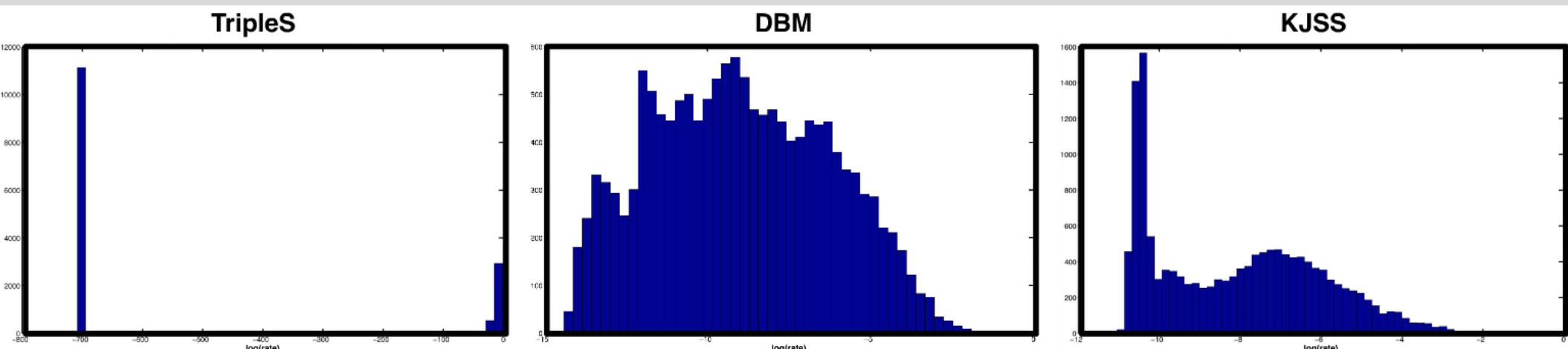


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### *Typical forecast distributions*

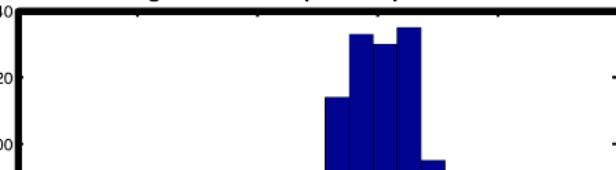


Example of  $\log(A)$  distribution (NW Pacific 2009)

### TripleS-TripleS

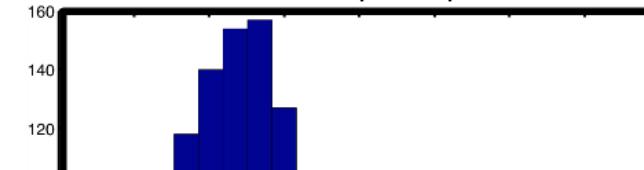
#### Avg. Info. Gain

Igain biased TripleS-TripleS Nr.32



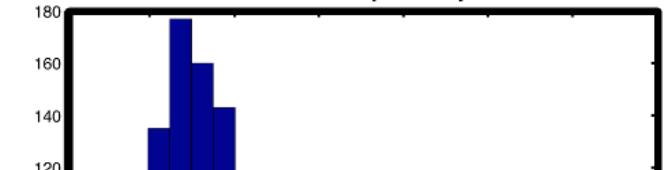
#### Student T-test

IConf T biased TripleS-TripleS Nr.32



#### Welch T-test

IConf TW biased TripleS-TripleS Nr.32

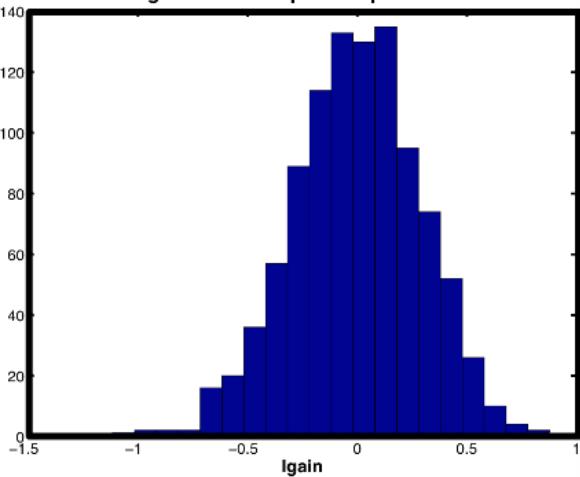


# Example of log(A) distribution (NW Pacific 2009)

## TripleS-TripleS

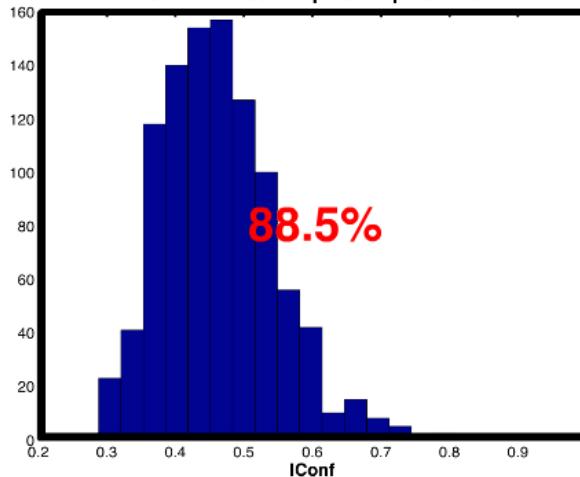
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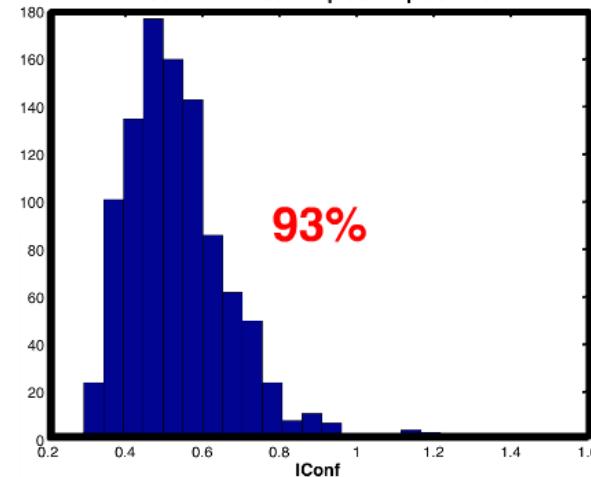
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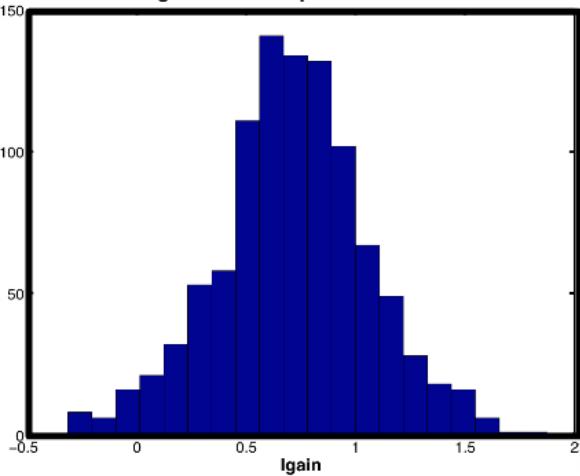


### W-test

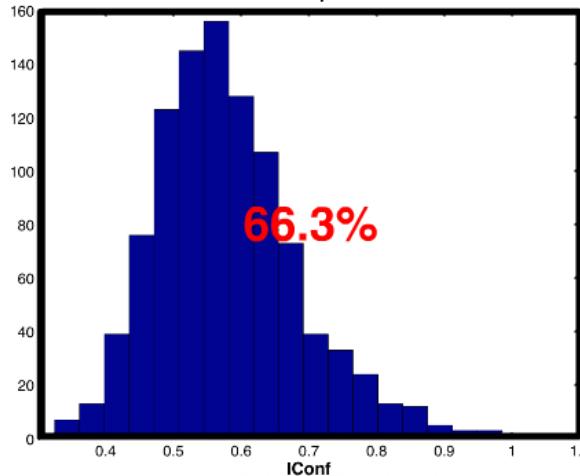
94.2%

## TripleS-DBM

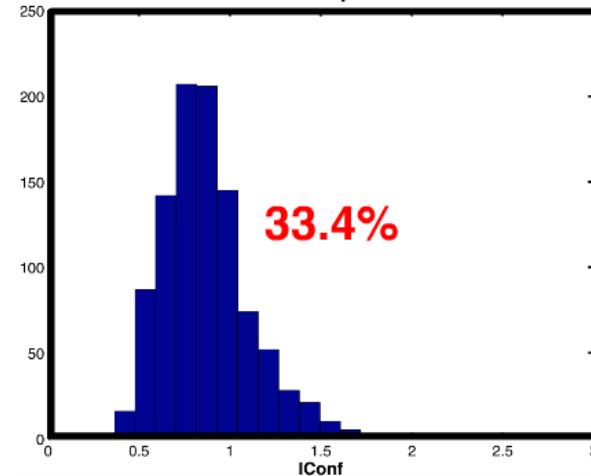
Igain biased TripleS-DBM Nr.32



IConf T biased TripleS-DBM Nr.32

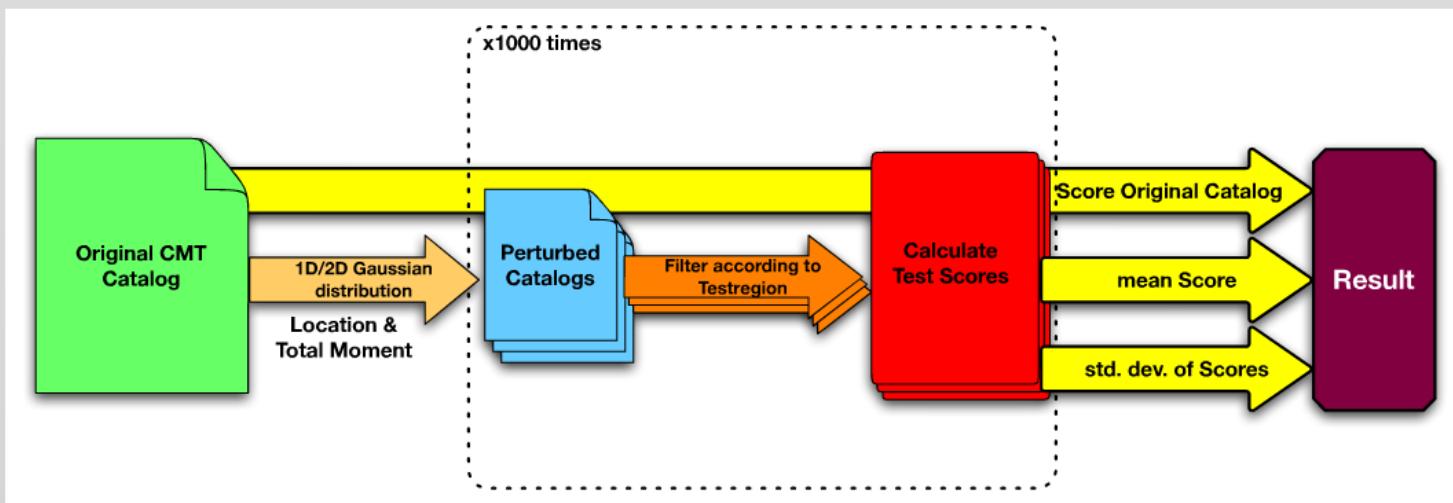


IConf TW biased TripleS-DBM Nr.32

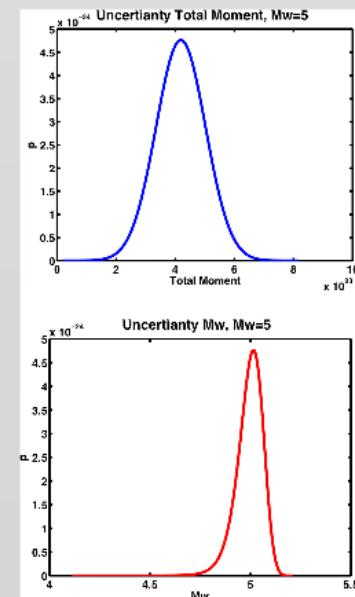


52.2%

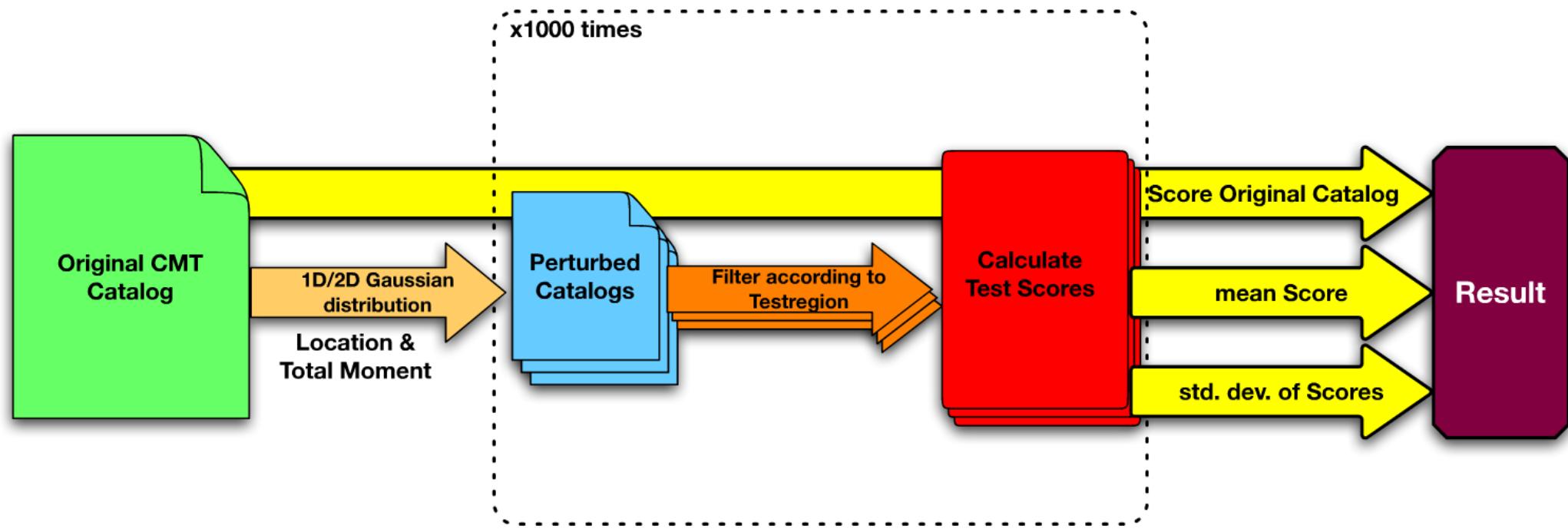
# *Uncertainty estimation*



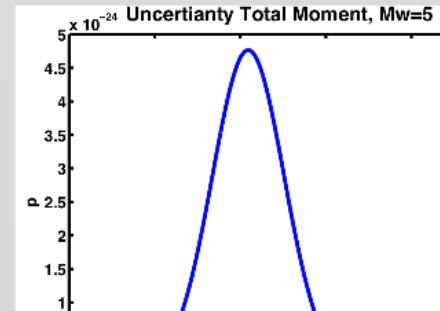
- Symmetric uncertainties in  $M_0$  - asymmetric uncertainties in  $M_w$
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# *Uncertainty estimation*



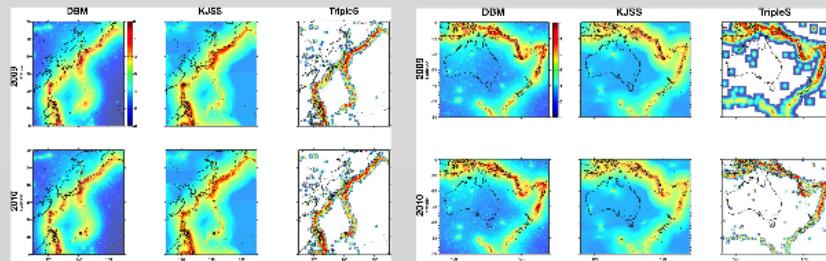
symmetric uncertainties in M0 - asymmetric  
uncertainties in Mw



# West Pacific Testing Region

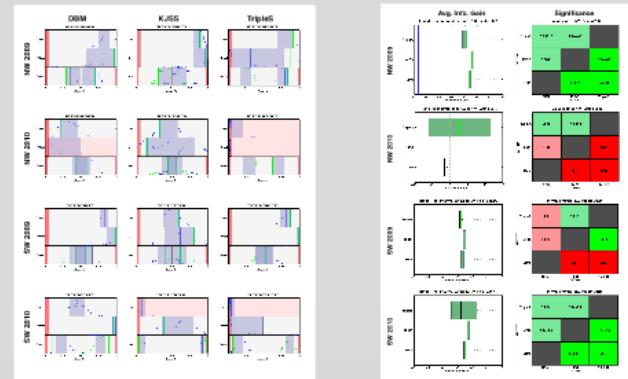
## Setup

- Two sub-regions for testing: NW and SW Pacific
- Current 2 one-year periods are used (2009 and 2010)
- Poisson rate forecasts from 3 Models:
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- M0 uncertainty CMT:  $0.2^*M0$

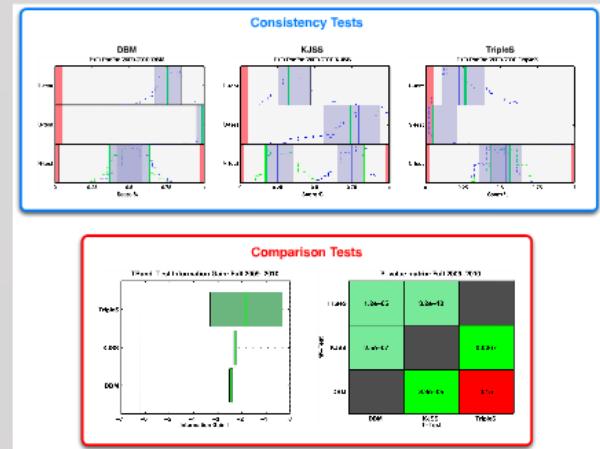


## Test Results

### "Single" Tests



### Test Summary

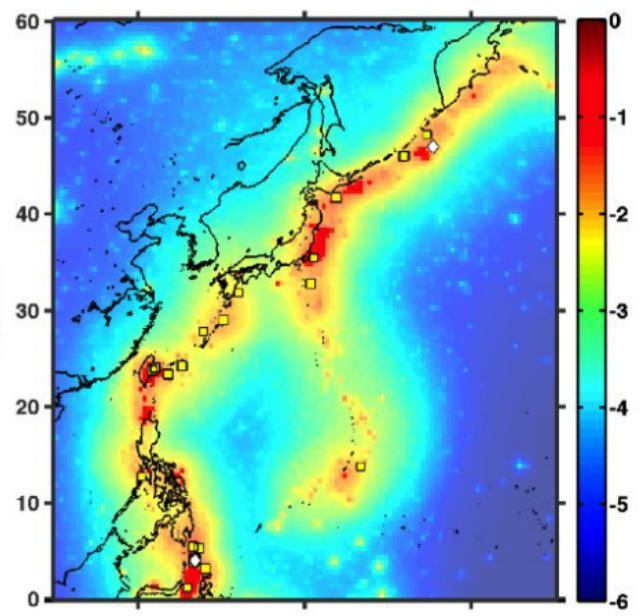
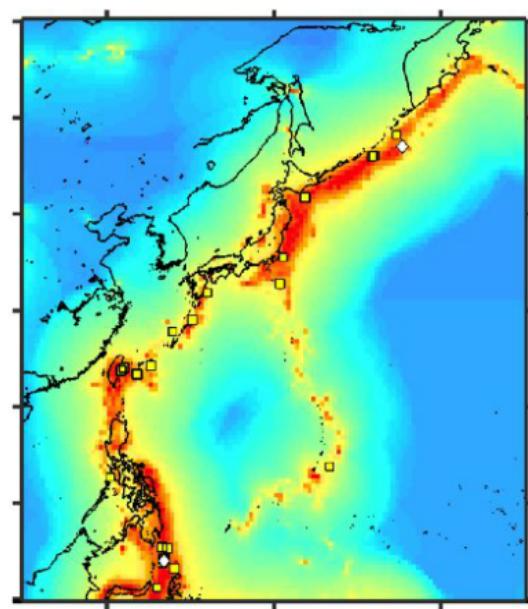
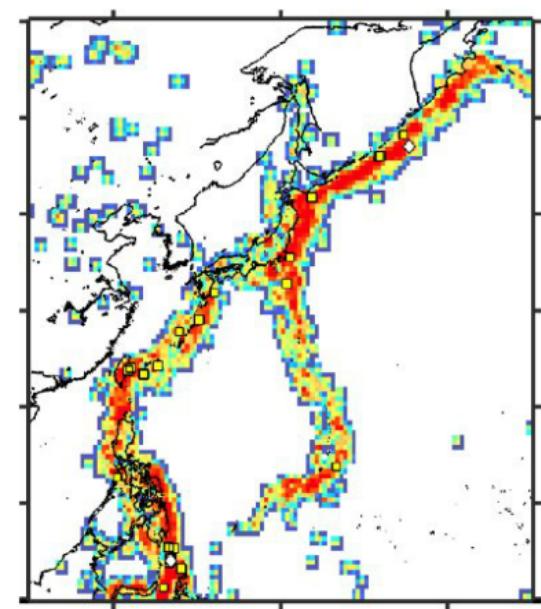


# *Setup*

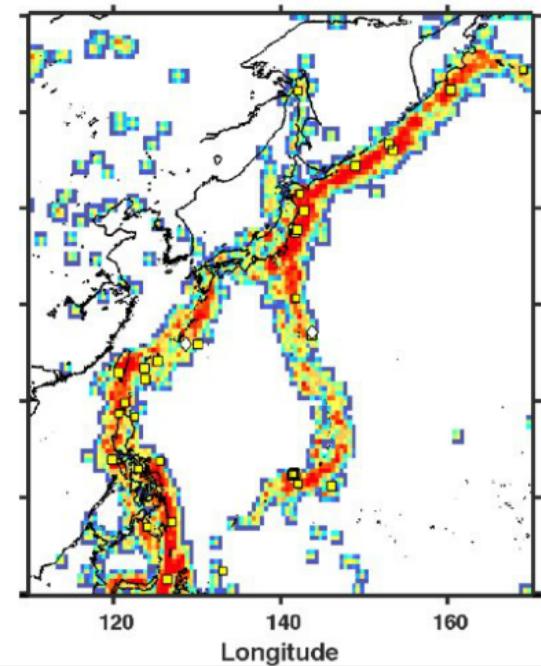
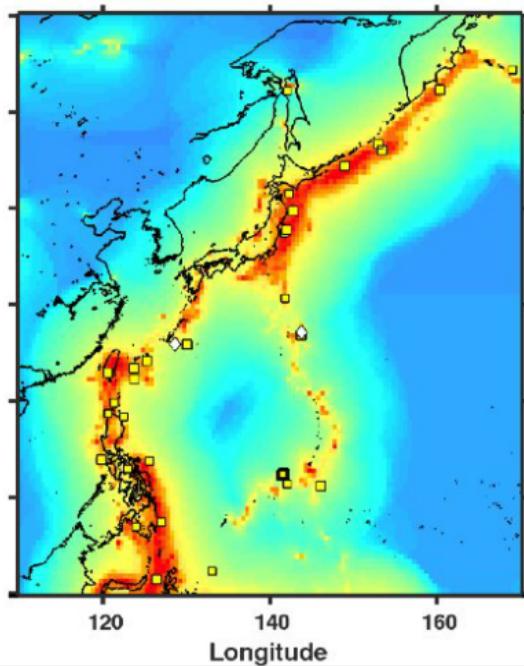
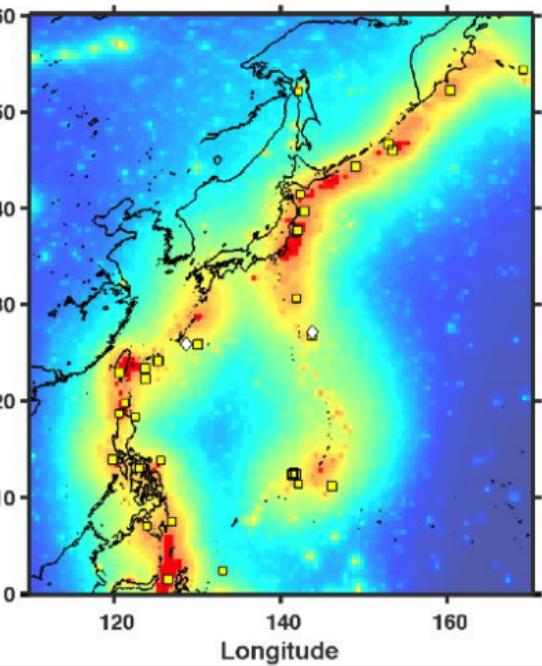
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2009

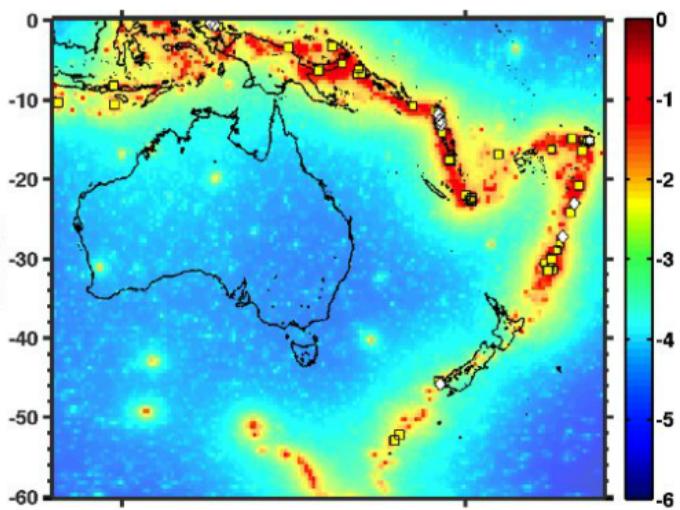
**DBM****KJSS****TripleS**

2010

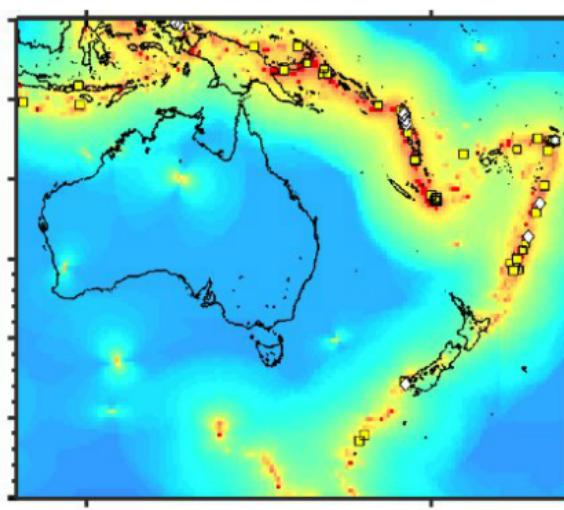


2009

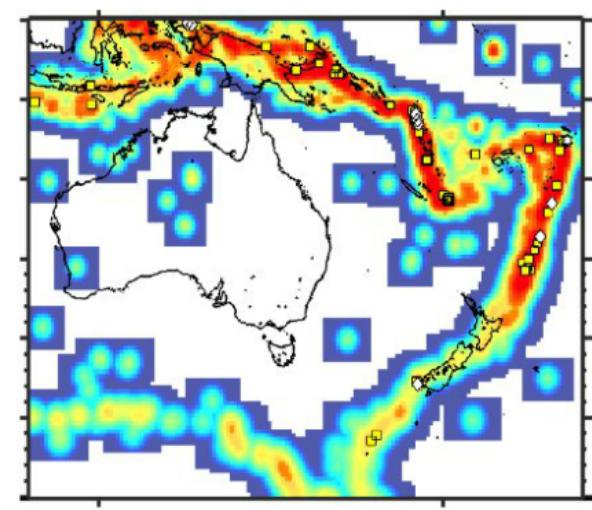
**DBM**



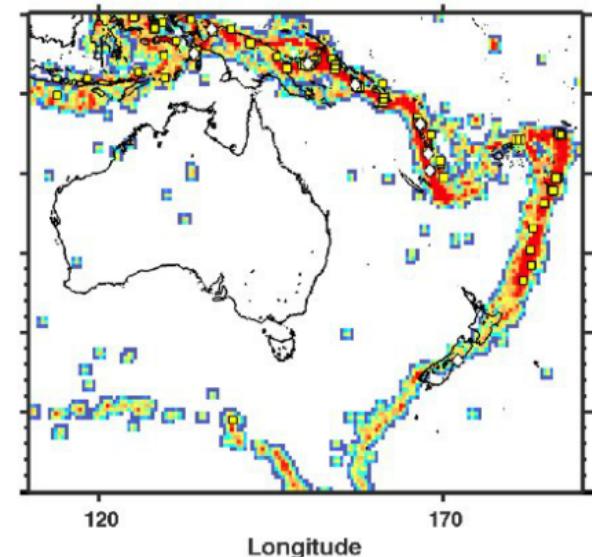
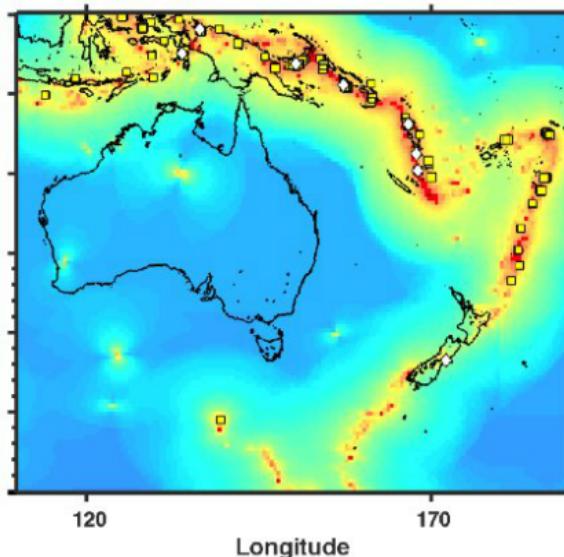
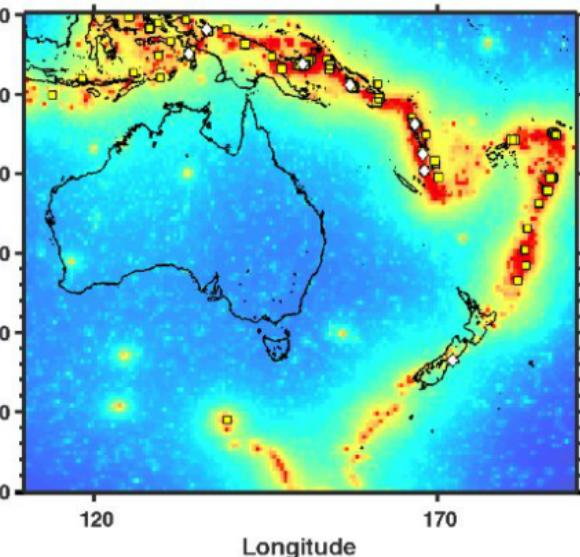
**KJSS**



**TripleS**



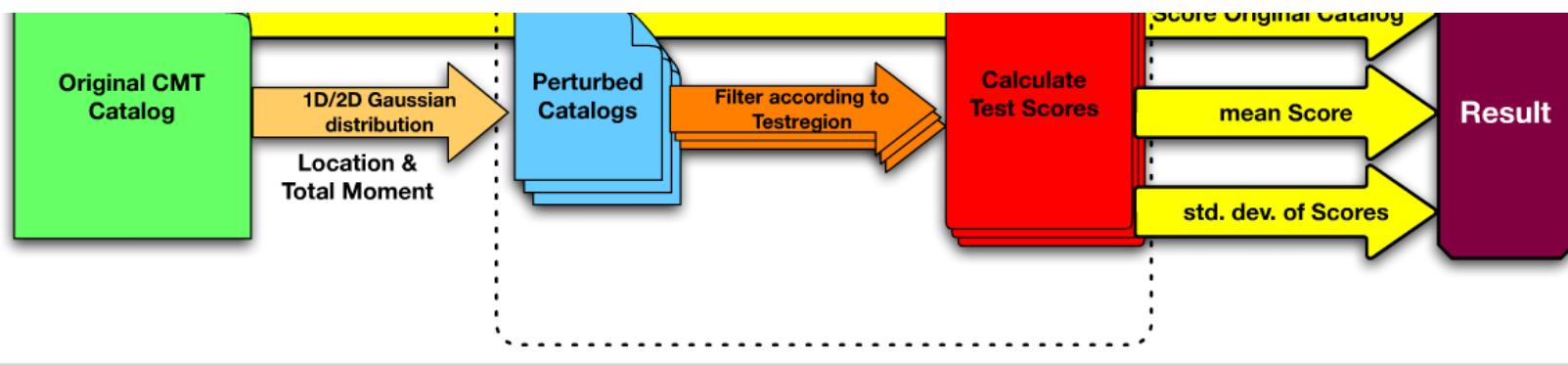
2010



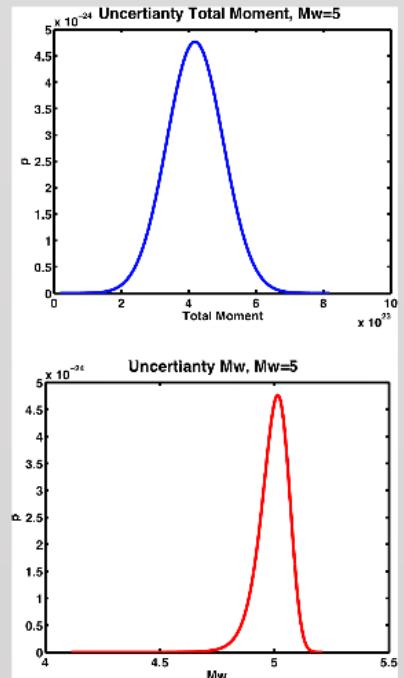
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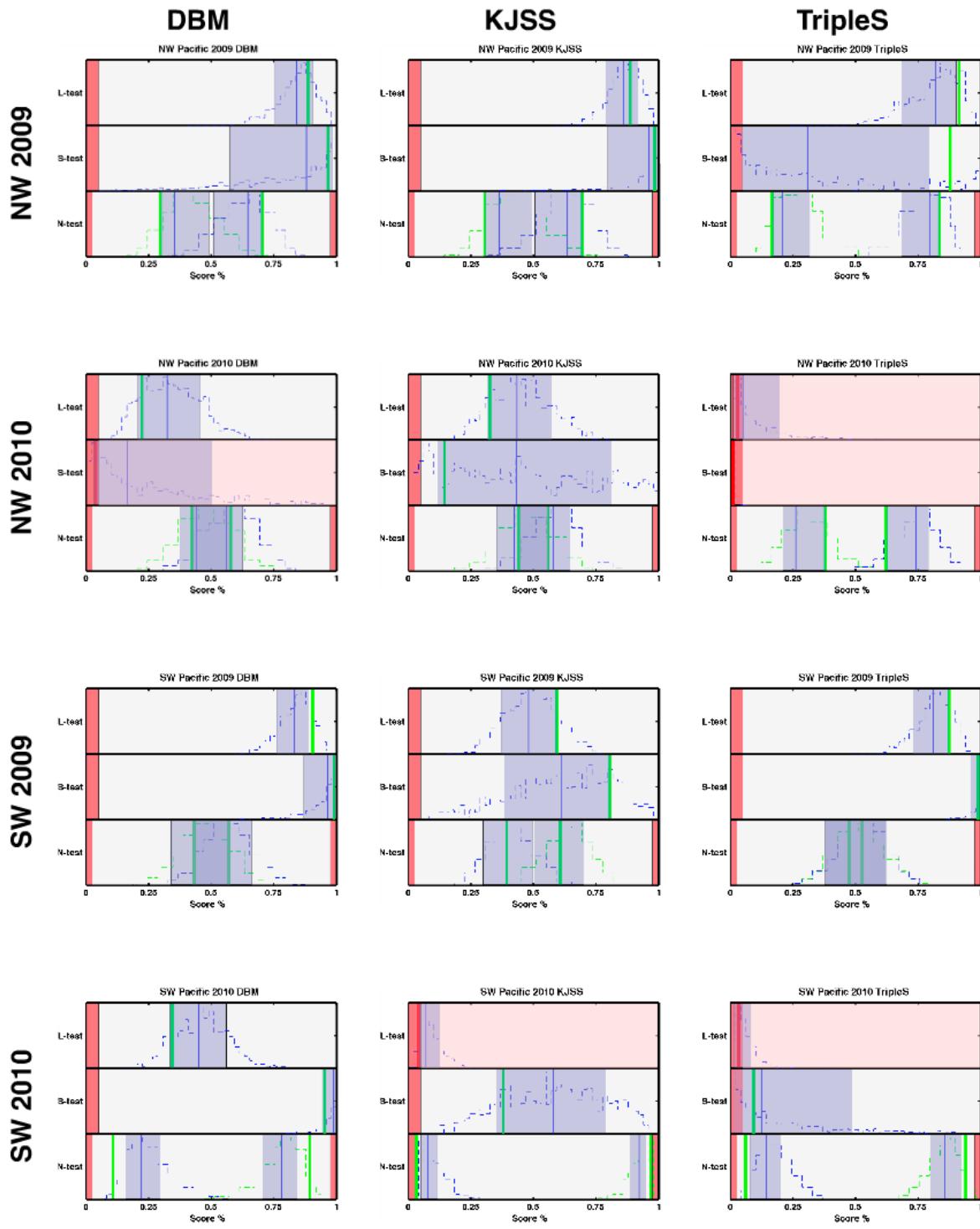
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NW 2009

NW 2010

SW 2009

SW 2010

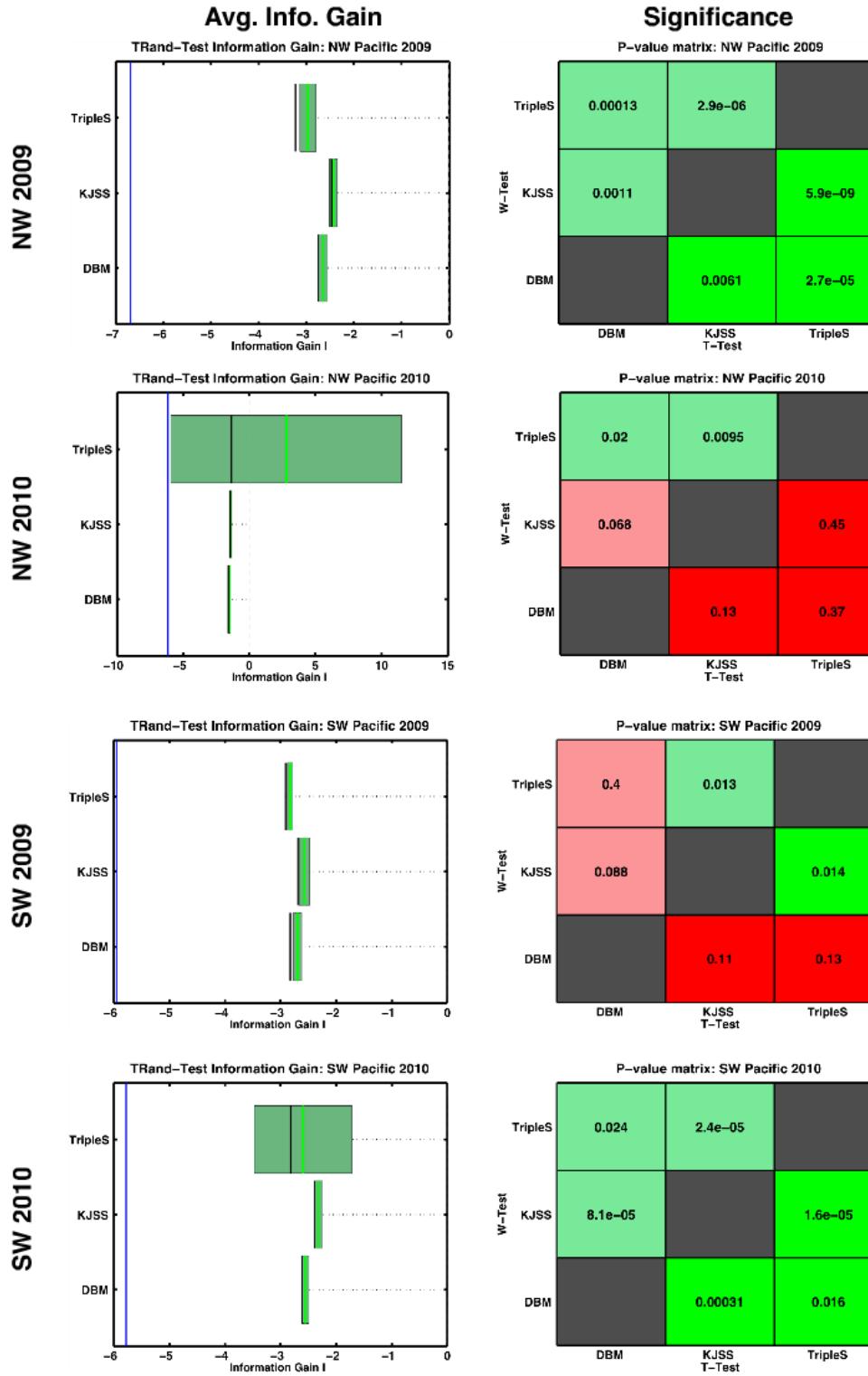
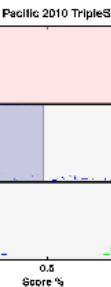
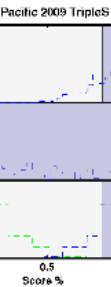
Triple  
KJS  
DB

Triple  
KJS  
DB

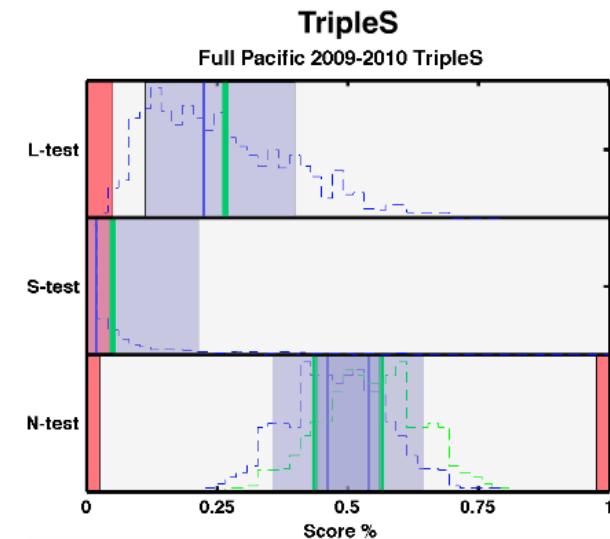
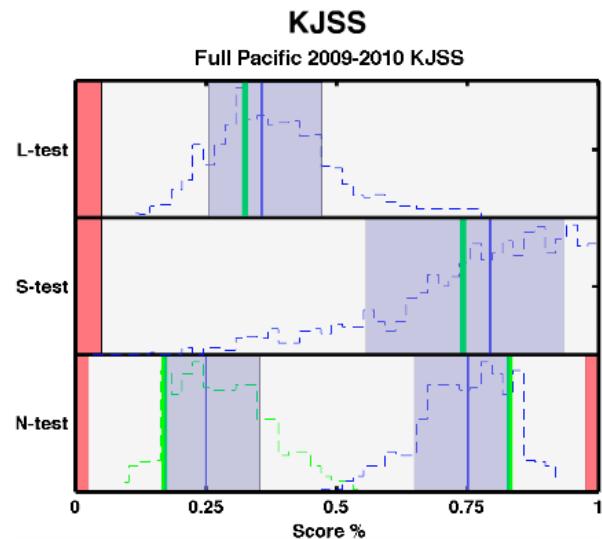
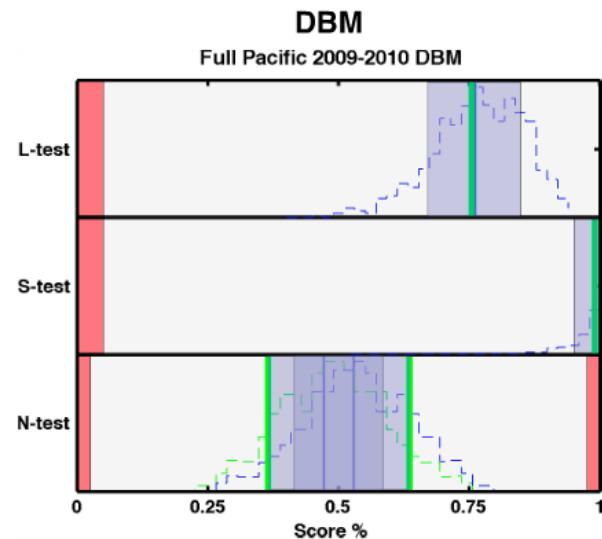
Triple  
KJS  
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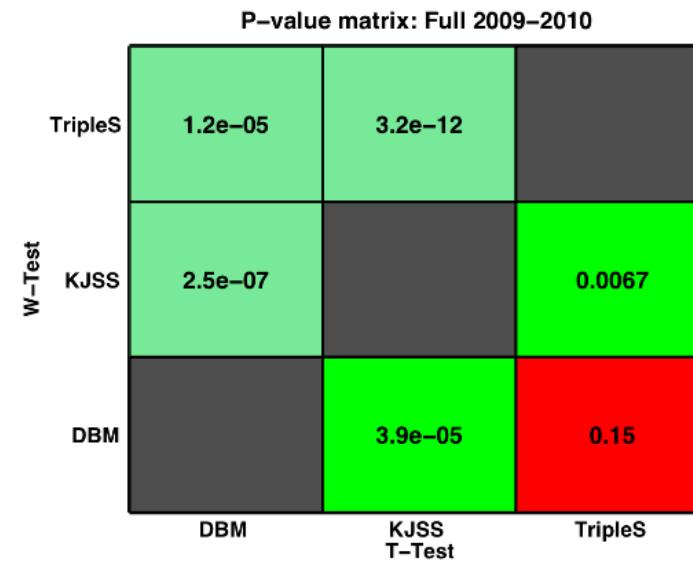
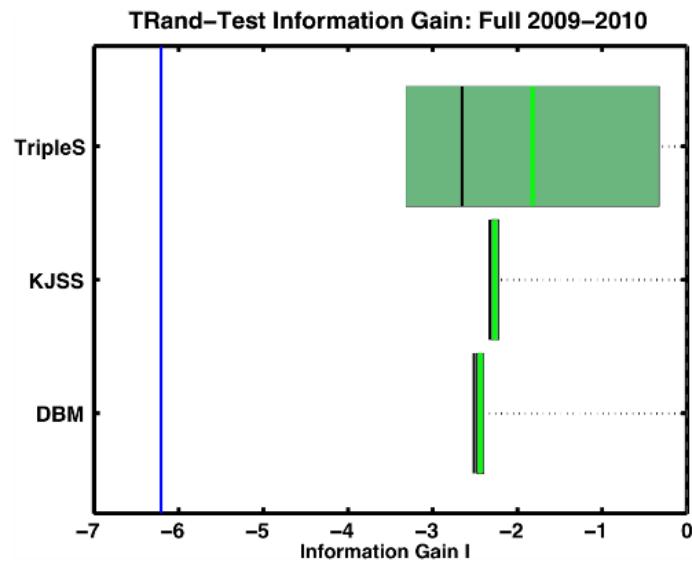
# triples



## Consistency Tests



## Comparison Tests



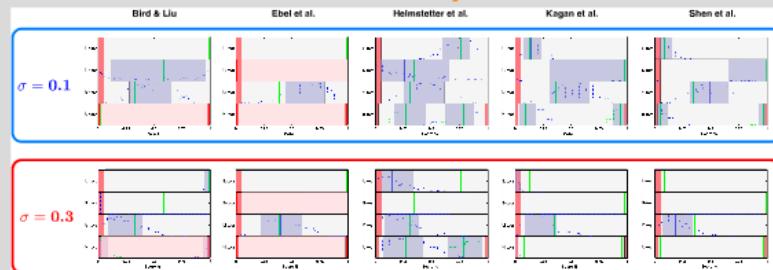
# Uncertainties in RELM

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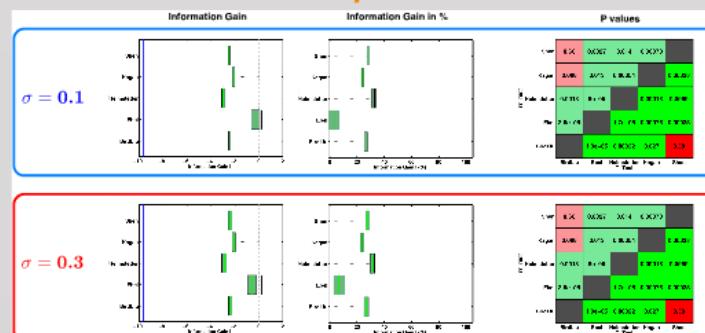
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  - Helmstetter et al.
  - Kagan et al.
  - Shen et al.
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  - Location uncertainties: 5 km
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- The ANSS Catalog did change between the first evaluation and this rework

## Test Results

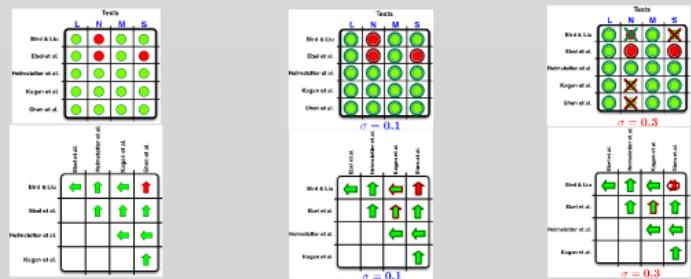
### Consistency



### Comparison



### "Original" vs Mean



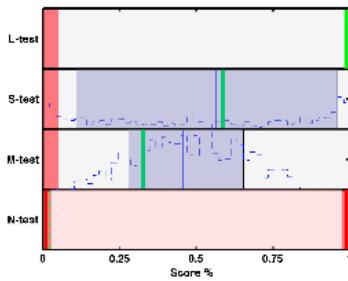
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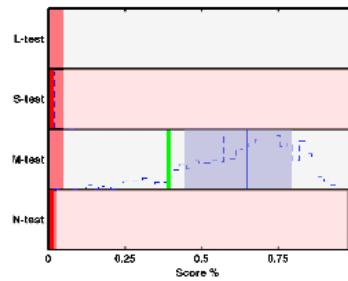
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## Consistency

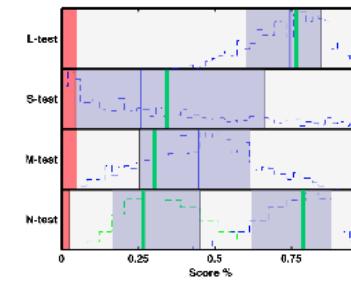
Bird & Liu



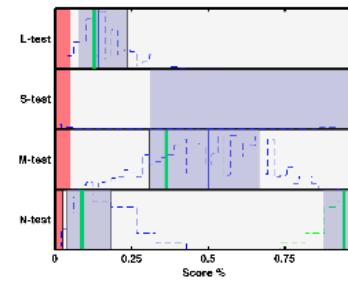
Ebel et al.



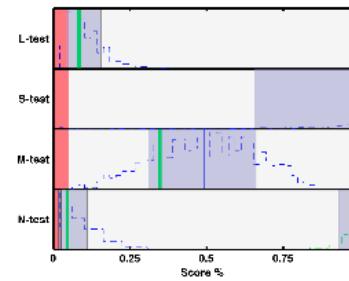
Helmstetter et al.



Kagan et al.



Shen et al.

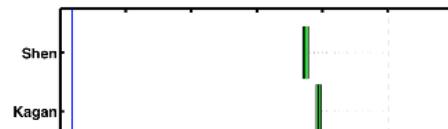


$\sigma = 0.1$

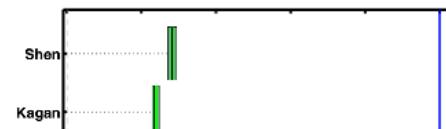
$\sigma = 0.3$

## Comparison

Information Gain

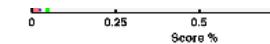


Information Gain in %



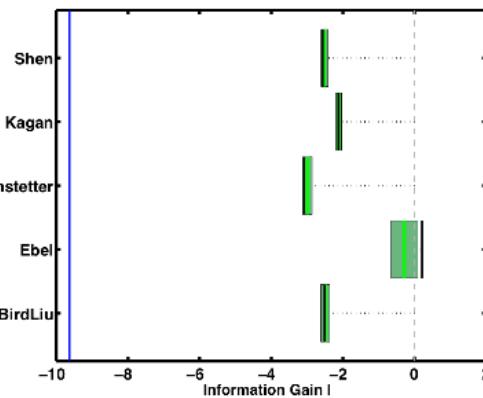
P values

|       |       |        |         |         |         |
|-------|-------|--------|---------|---------|---------|
| Shen  | 0.66  | 0.0027 | 0.014   | 0.00078 |         |
| Kagan | 0.088 | 0.013  | 0.00054 |         | 0.00033 |

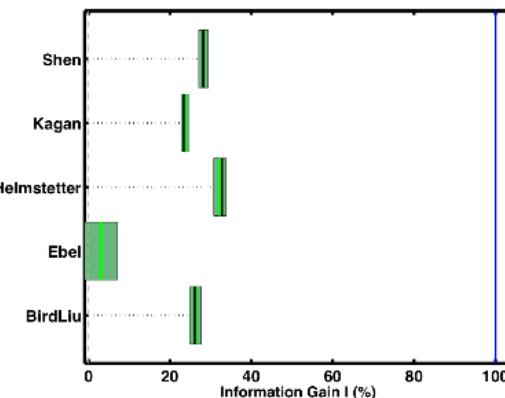


# Comparison

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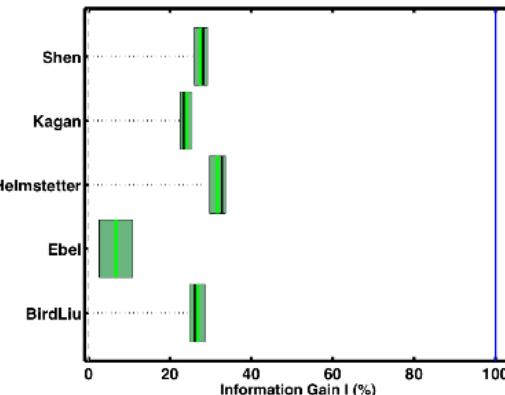
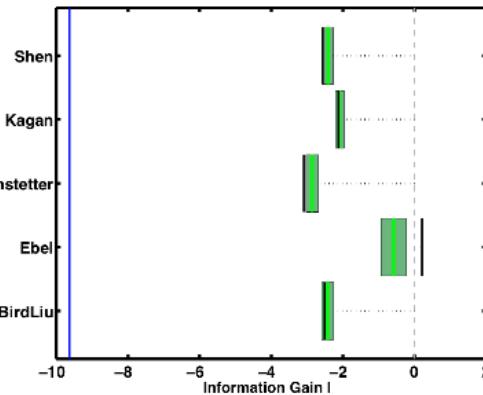
Information Gain in %



P values

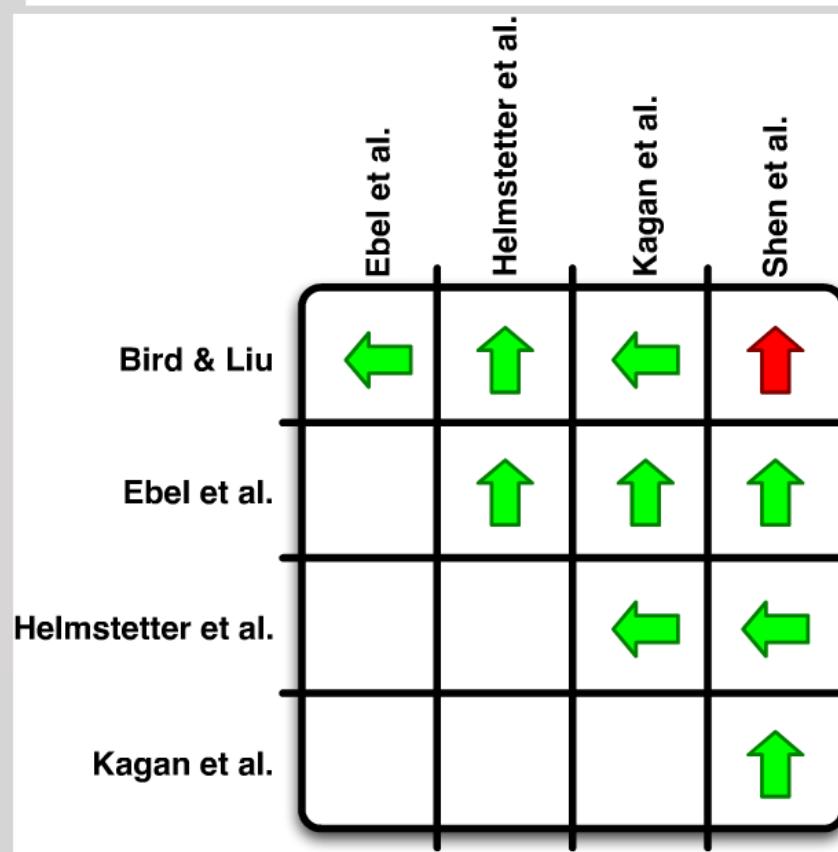
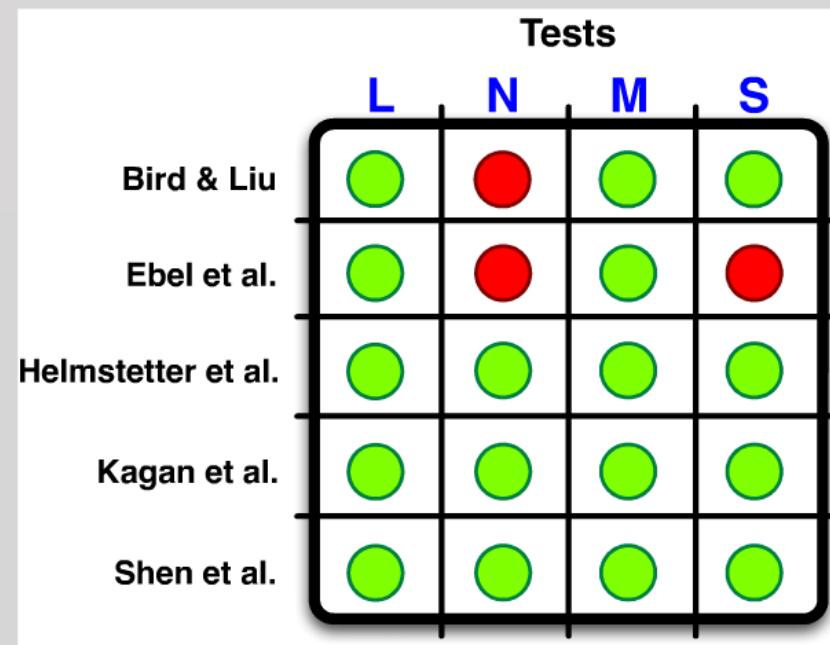
| W-Test      | BirdLiu | Ebel    | Helmstetter | Kagan   | Shen    |
|-------------|---------|---------|-------------|---------|---------|
| Shen        | 0.66    | 0.0027  | 0.014       | 0.00078 |         |
| Kagan       | 0.088   | 0.013   | 0.00054     |         | 0.00033 |
| Helmstetter | 0.0013  | 6e-05   |             | 0.00013 | 0.0089  |
| Ebel        | 3.8e-05 |         | 1.7e-05     | 0.00075 | 0.00035 |
| BirdLiu     |         | 1.9e-05 | 0.00022     | 0.027   | 0.38    |

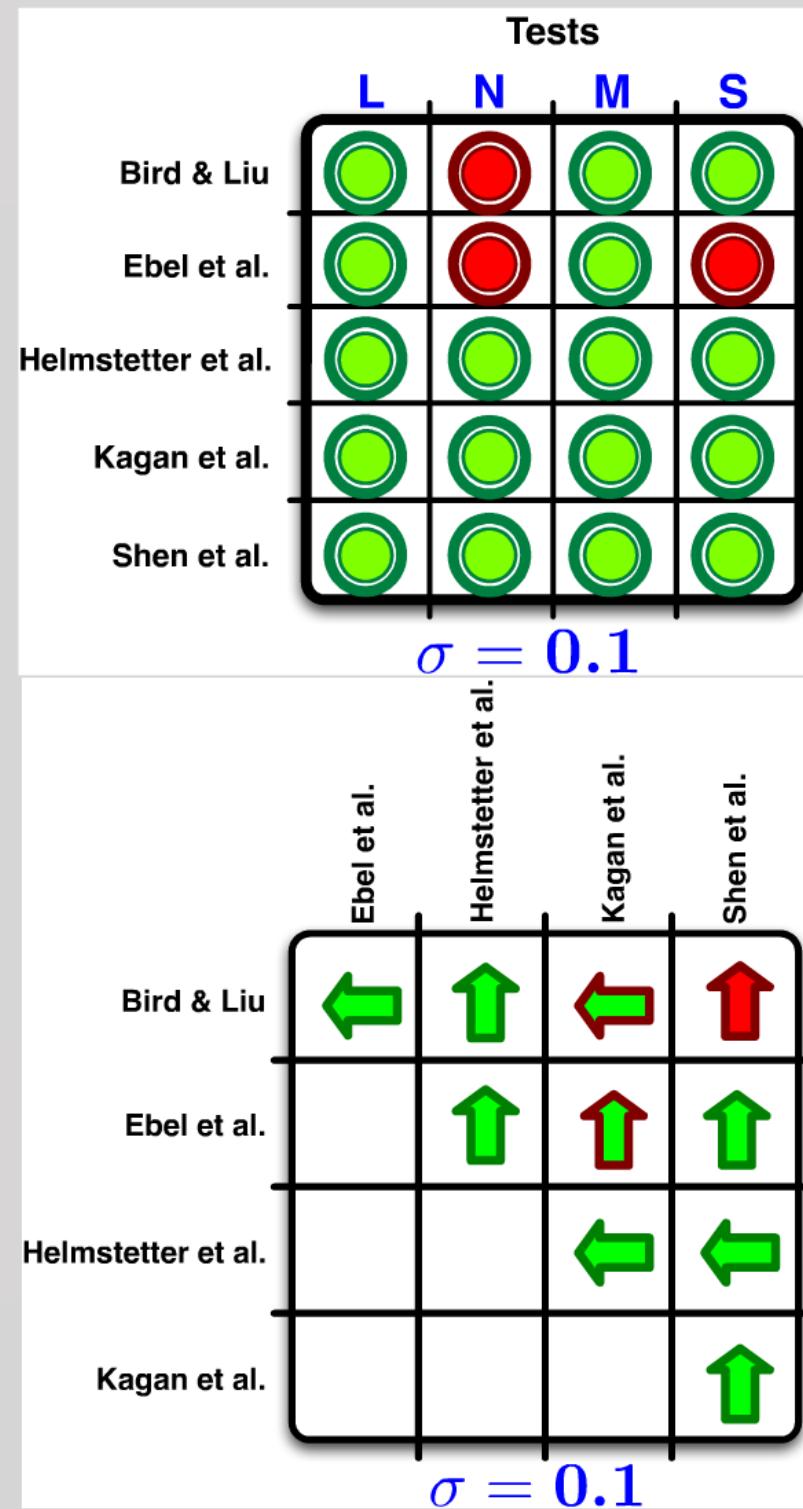
$\sigma = 0.1$

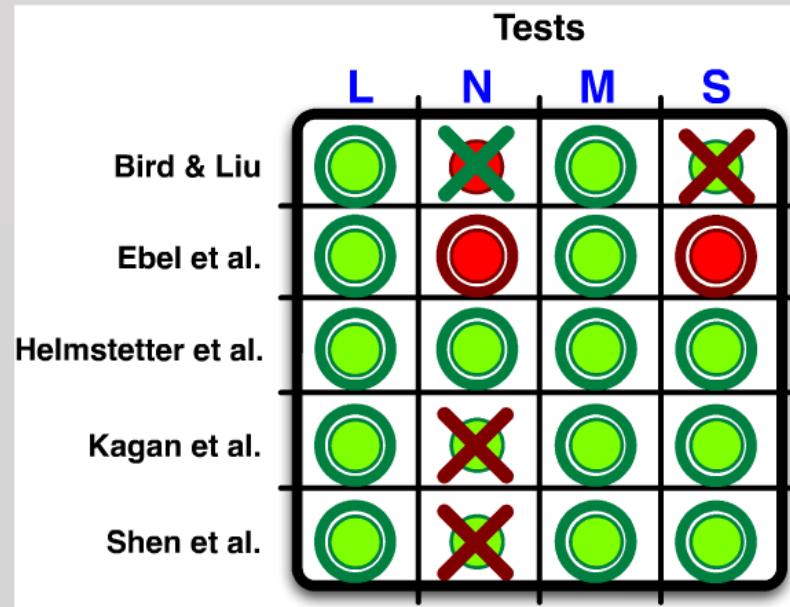


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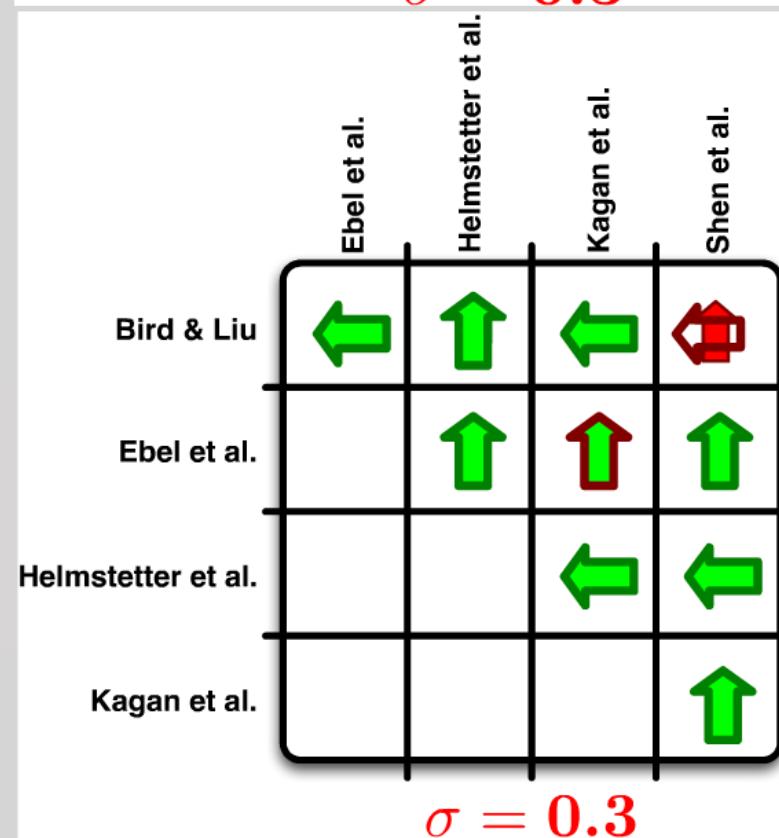
*"Original"* vs Mean







$$\sigma = 0.3$$



# *Unfinished Business*

## *CSEP West Pacific*

- 2 years of data are not enough, addition 1 year periods will be added
- 3 models are a start but not enough
- Magnitudes bins are missing and successor test regions like the global test region should consider them.

## *Accounting for Uncertainties*

- The effect on the test outcome is dependent on the forecast and the location of the earthquakes
- Can help to evaluate the robustness of forecast for a certain test region and time period
- Uncertainty estimation is a valuable addition to the test procedure

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